



CAUSE

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TECHNOLOGY



# Machines Climbing Pearl's Ladder of Causation

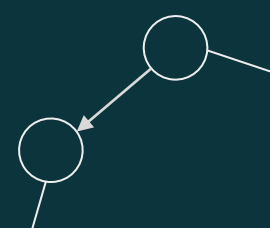
Devendra Singh Dhami  
Adele Ribeiro  
Matej Zečević



ESSAI & ACAI 2024

ATHENS - GREECE

Machines Climbing Pearl's Ladder of Causation





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- PhD Candidate at Technical University of Darmstadt

## 5 Thrilling Days

- Day 1: Introduction to Causality (Devendra)
- Day 2: Causal Discovery (Adèle)
- Day 3: Causal Identification and Estimation (Adèle)
- Day 4: Causal Representation Learning (Devendra)
- Day 5: Causality + Large Language Models (Devendra)

# Disclaimer



*"Don't be fooled. Chaos reigns."*



# The Ultimate Hitchhiker's Introduction to Causality for ML

Devendra Singh Dhami





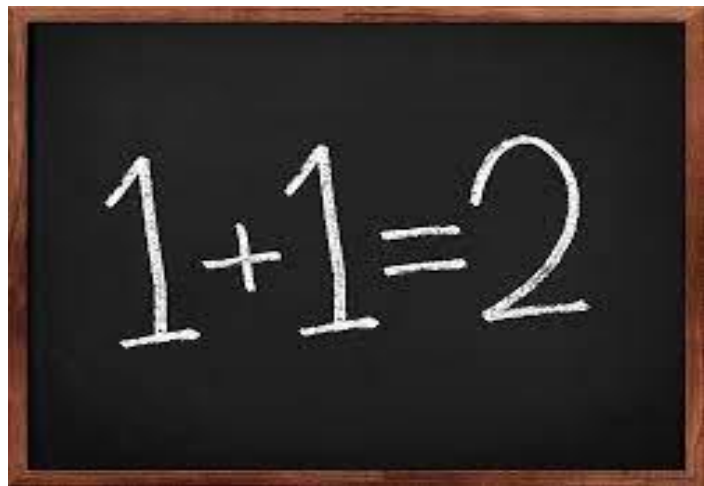
KMBC  
NEWS 9

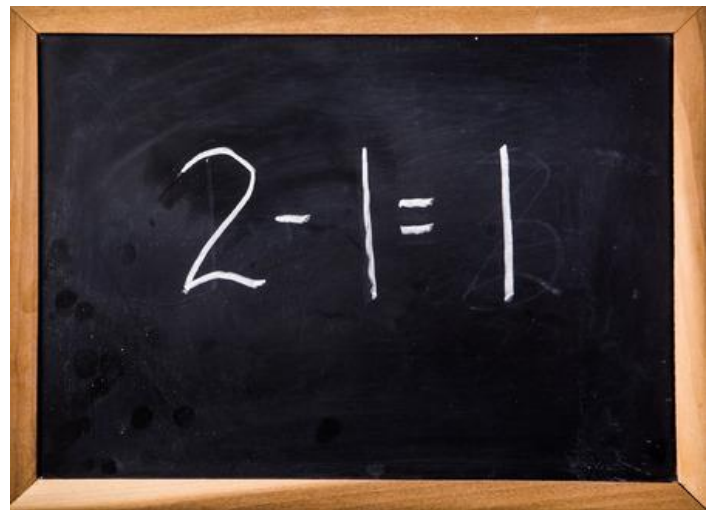






Causality is hard

A square chalkboard with a wooden frame. The equation  $1+1=2$  is written in white chalk on a black background.
$$1+1=2$$

A square chalkboard with a wooden frame. The equation  $2-1=1$  is written in white chalk on a black background.
$$2-1=1$$

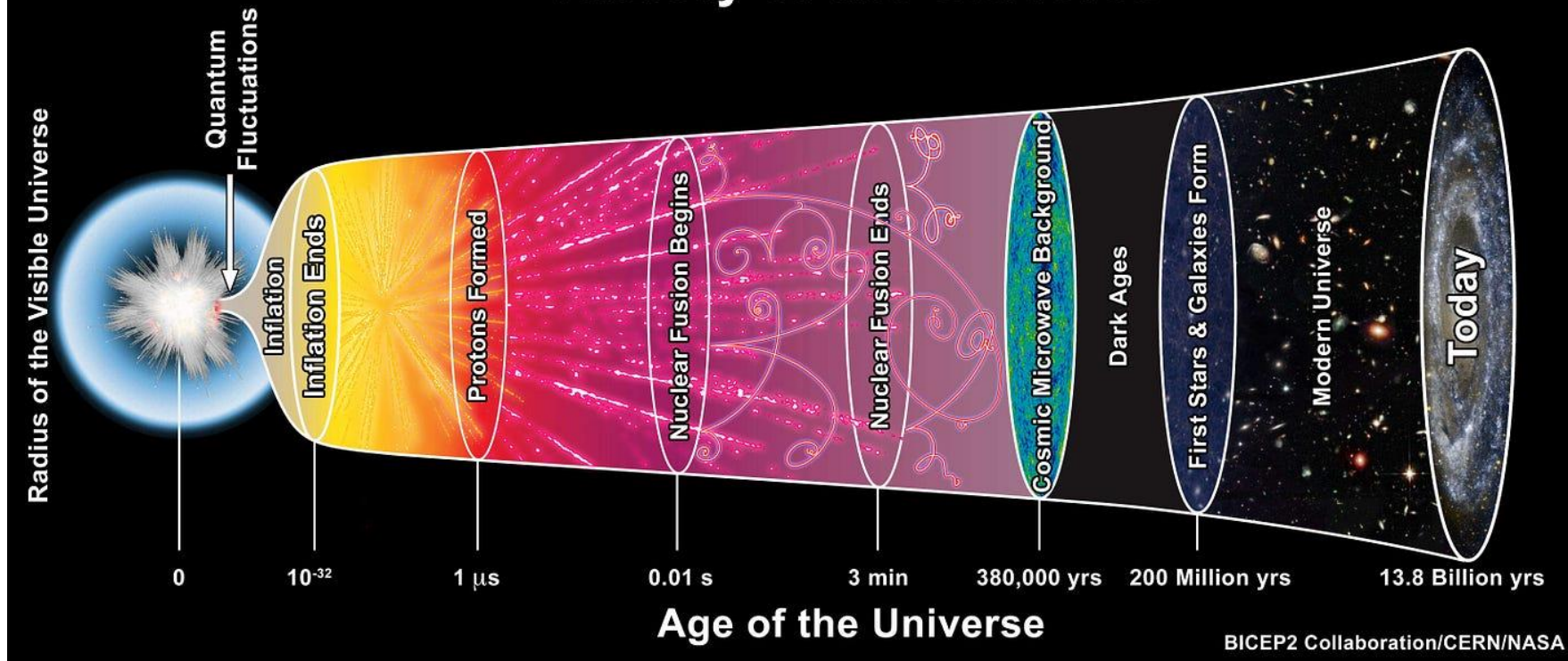
Causality is hard(er)



Causality is hard(er)



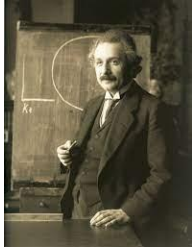
# History of the Universe



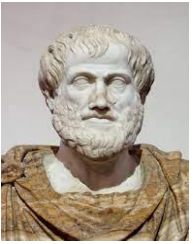
BICEP2 Collaboration/CERN/NASA

Carl Sagan: If you wish to make an apple pie from scratch, you must first invent the universe

# Causality is Omnipresent!



**Classical Physics:** An effect cannot occur from a cause that is not in the back (past) light cone of that event. Similarly, a cause cannot have an effect outside its front (future) light cone



**Philosophy:** The material cause of a being is its physical properties or makeup. The formal cause is the structure or direction of a being. The efficient cause is the thing or agent, which actually brings it about. And the final cause is the ultimate purpose for its being

The Sveriges Riksbank Prize in  
Economic Sciences in Memory of  
Alfred Nobel 2021



©. Niklas Elmehed © Nobel Prize  
Outreach  
David Card  
Prize share: 1/2

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Outreach  
Joshua D. Angrist  
Prize share: 1/4

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Outreach  
Guido W. Imbens  
Prize share: 1/4

**Economics:** Develops explicit models of outcomes where the causes of effects are investigated and the mechanisms governing the choice of treatment are analyzed

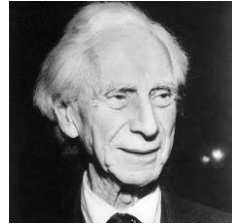
# Causality is Omnipresent?

**David Hume:** Causation is a relationship between two impressions or ideas in the mind. Because causation is defined by experience, any cause-and-effect relationship could be incorrect because thoughts are subjective and therefore causality cannot be proven



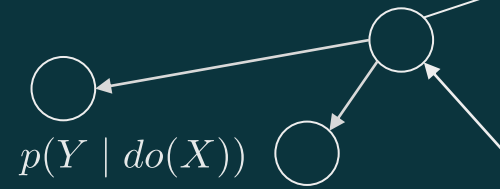
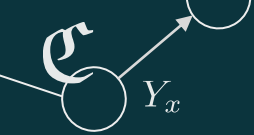
**Barber's Paradox:** There is a village where the barber shaves all those and only those who do not shave themselves. Who shaves the barber?

A causal problem → Are the non-shavers actually non-shavers because they're shaved by the barber or whether they're shaved by the barber because they're non-shavers. If the first is true, the barber is a member of both groups: he shaves himself and is shaved by the barber



Can you define  
“What is Causality?”

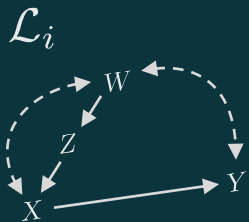


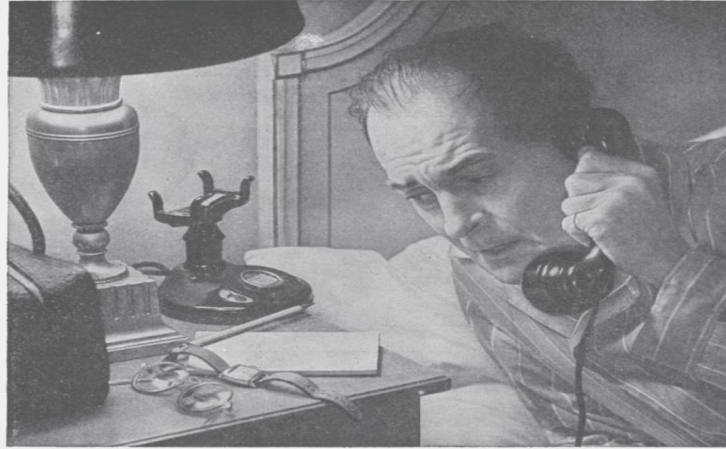


# I

# Why?

Machine Learning needs Causality?





## “I’ll Be Right Over!”

*... 24 hours a day your doctor  
is “on duty”... guarding  
health... protecting and  
prolonging life...*

• Plays... novels... motion pictures... have been written about the “man in white.” But in his daily routine he lives more drama, and displays more devotion to the oath he has taken, than the most imaginative mind could ever invent. And he asks no special credit. When there’s a job to do, he does it. A few winks of sleep... a few puffs of a cigarette... and he’s back at that job again...

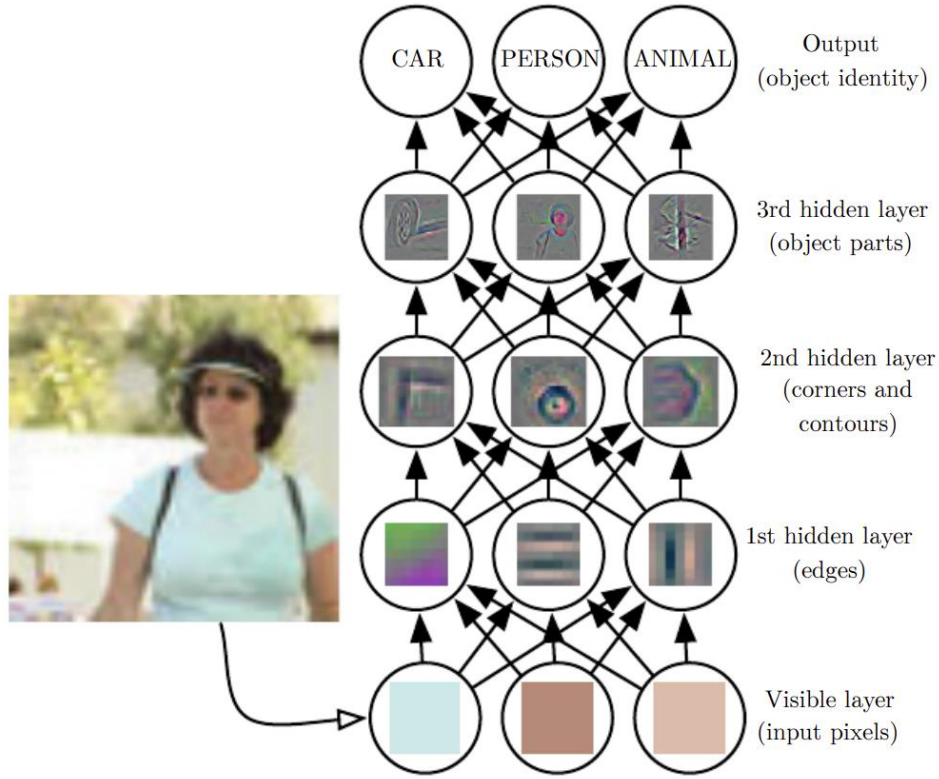


R. J. Reynolds Tobacco Company, Winston-Salem, N. C.

According to a  
recent independent  
nationwide survey:

**More Doctors  
Smoke Camels**  
*than any other cigarette*

# Current Trend: Deep Learning



# Current Trend: Deep Learning

DE

an example causal graph for unexperienced audience



Sure! Let's create a simple causal graph with an example that is easy to understand for an inexperienced audience. Suppose we want to demonstrate the relationship between sleep and academic performance in students.

Example Causal Graph: Sleep and Academic Performance

In this example, we have two variables: "Sleep" and "Academic Performance." We will use arrows to represent causal relationships between these variables.

```
scss Copy code
+-----+
|      |      |
|  Sleep  |      |
|      |      |
+---(causes)----> +---(causes)---->
|      |      |
|      |      |
+-----+      Academic
                        Performance
```

# Current Trend: Deep Learning

Explanation:

1. Sleep: This variable represents the number of hours a student sleeps each night.
2. Academic Performance: This variable represents a student's academic performance, which can be measured by their grades or exam scores.

Causal Relationship:

The arrow pointing from "Sleep" to "Academic Performance" indicates a causal relationship. In this example, we are hypothesizing that sleep directly affects academic performance. More sleep may lead to better academic performance, while less sleep may result in poorer academic performance.

# Current Trend: Deep Learning



# Current Challenges in DS, AI, ML

COVID-19 IMAGING WOMEN'S HEALTH

nature  
Explore content

nature > outlook > article  
**A fairer world**

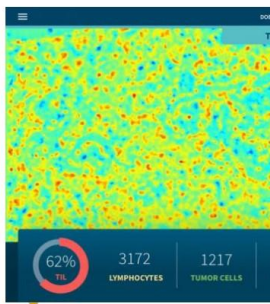
Without careful intervention, artificial intelligence will exacerbate health inequality.  
Linda Nordling



NEWS | ARTIFICIAL INTELLIGENCE | MARCH 22, 2021

## Making the Role of AI in Breast Cancer Diagnosis Fairer

Analysis system for the diagnosis of breast cancer



Detection of tumor-infiltrating lymphocytes (TILs) generate a heatmap showing TILs (red) and other tumor cells (yellow/green) of Klauschen/Charité

MIT Technology Review

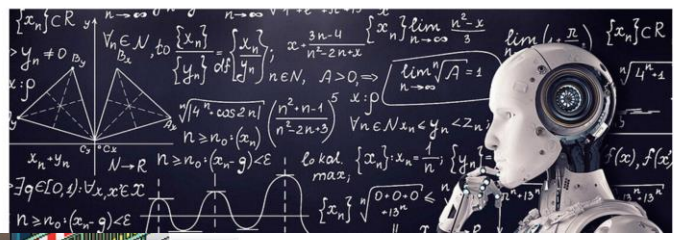
Artificial intelligence  
**What AI**

Artificial intelligence struggles to grasp cause and effect with.

by **Brian Bergstein**

This article was published on March 21, 2021

## Why AI struggles to grasp **cause and effect**



### POPULAR ON NEURAL TODAY

- 1 Physicists working with Microsoft think the universe is a self-learning computer
- 2 NASA just made history by flying an autonomous helicopter on Mars

# Current **Challenges** in DS, AI, ML

- Data-hungry & sample inefficiency
- Lack of interpretability & explainability
- Lack of robustness & generalizability
- Unfair & unethical decision-making



Lack of Causal Inference Capabilities



# What can we achieve with causality?

**Data Fusion:** provides language and theory to cohesively combine prior knowledge and data from multiple and heterogeneous studies.

**Effect identifiability:** can determine the effect of unrealized interventions rather than just predicting an outcome (i.e., can distinguish between association and causation)

**Generalizability:** allows the transportability of causal effects across different domains.

**Explainability:** provides a better understanding of the underlying mechanisms.

**Fairness:** captures and disentangles any mechanisms of discrimination that may be present, including direct, indirect-mediated, and indirect-confounded.



Prompt: Make it a dark **start-lit** night.



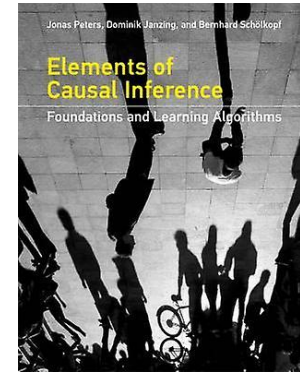
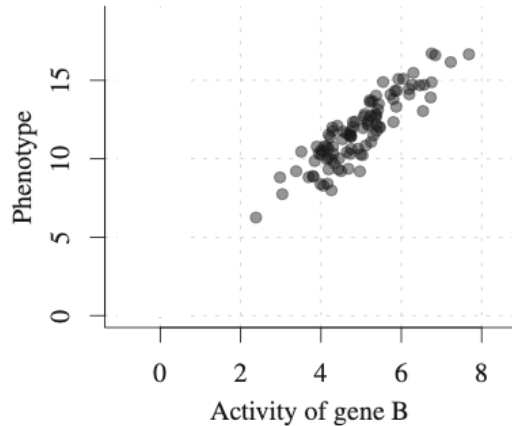
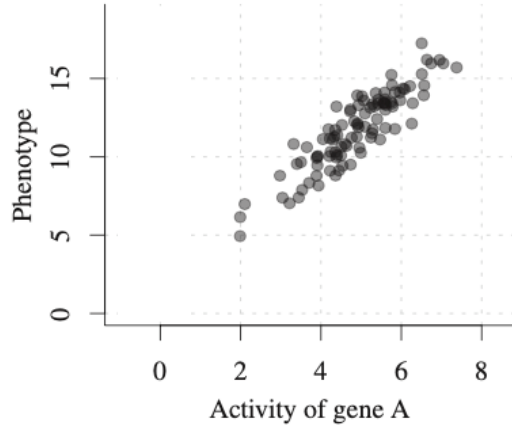
Prompt: Make it a dark **star-lit** night.



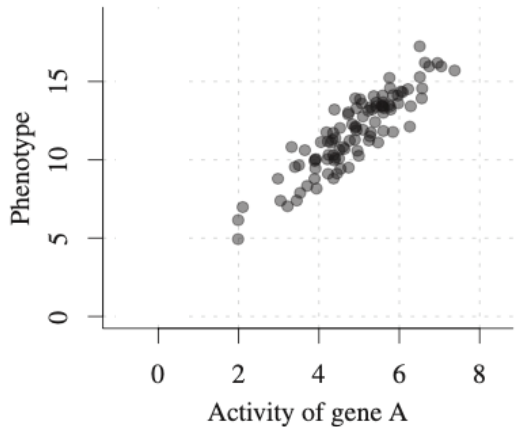
Prompt: Make it a dark **star-lit** night.

Why do we care about  
causality in AI & ML?

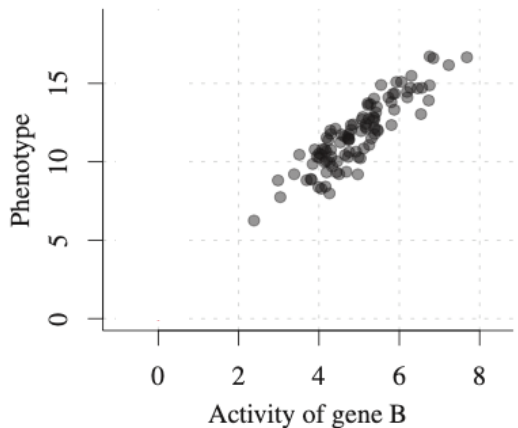
In ML for instance,  
we'll encounter data  
sets like on the left...



Dataset I

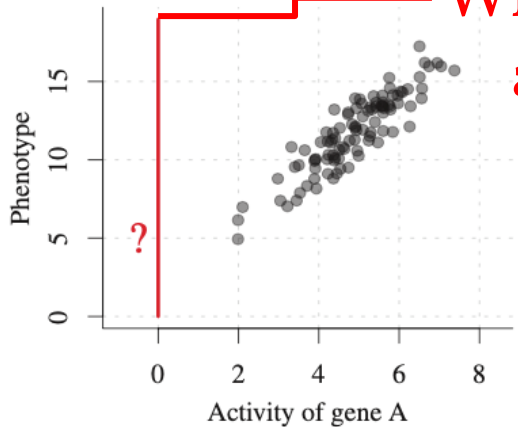


Dataset II



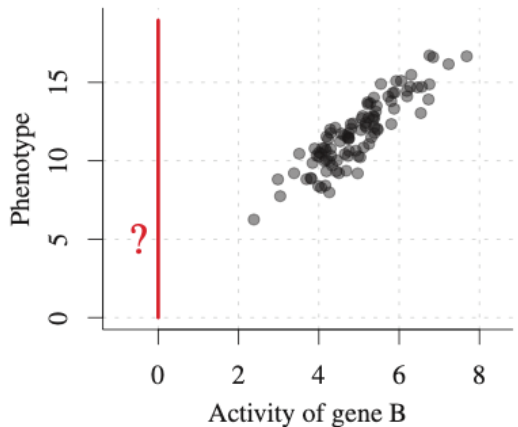
But, what is the difference between datasets I & II w.r.t. learning?

Dataset I



What if we kill the activity of the gene?

Dataset II

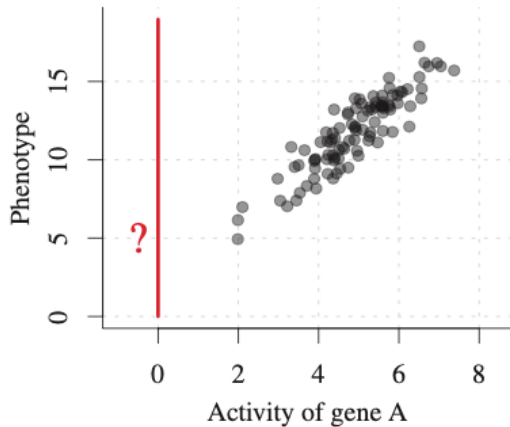


We might ask about the difference w.r.t. generalization!

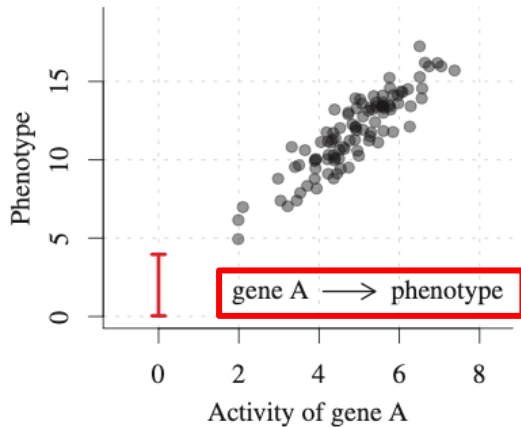


What if we kill the activity of the gene?

Dataset I

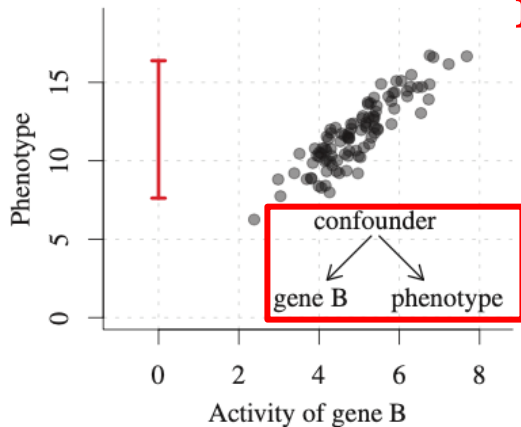
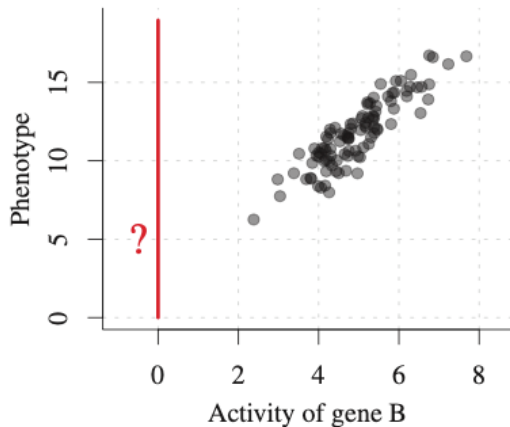


Then we expect the following range



the difference is  
in the underlying  
**Causality!**

Dataset II



In Conclusion:

Without considering causality, the best  
that our algorithms could do is to say  
“I don’t know”\*

\* and we really really really do want to know

Causality allows us to talk about **modelling assumptions**

Causality allows us to consider not just the joint distribution but the **data generating process** which induces said distribution

# What is Causality?

We might want to start here first..

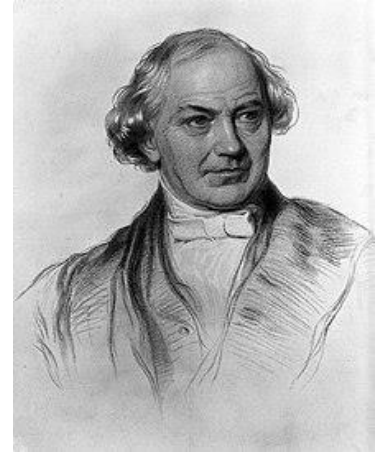


Probably, Plato was the first to state the principle of causality:

“Everything that becomes or changes must do so owing to some cause; for nothing can come to be without a cause.” - *Timaeus* 28a

# Axioms of Causality

- Nothing takes place without a cause.
- The magnitude of an effect is proportional to the magnitude of its cause.
- To every action there is an equal and opposed reaction.

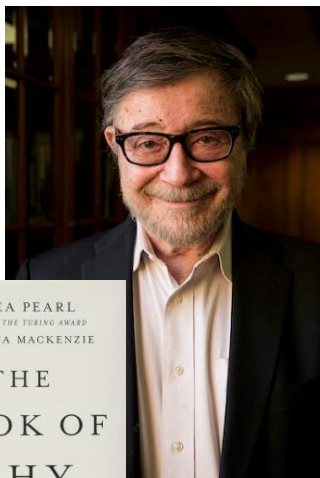


Example: if a baseball is moving through the air, it must be moving this way because of a previous interaction with another object, such as being hit by a baseball bat

**Principle of Universal Causation:** Every phenomenon has a cause, which it invariably follows; and from this are derived other invariable sequences among the successive stages of the same effect, as well as between the effects resulting from causes which invariably succeed one another

# Judea Pearl's opinion

Pioneer of Causality for AI, Turing awardee



“To Build Truly Intelligent Machines,  
Teach Them Cause and Effect”

“All the impressive achievements of deep learning  
amount to just curve fitting”

Judea Pearl in “The Book of Why”  
and in an interview with quanta magazine in 2018

# Yoshua Bengio's opinion

Pioneer of Deep Learning, Turing awardee



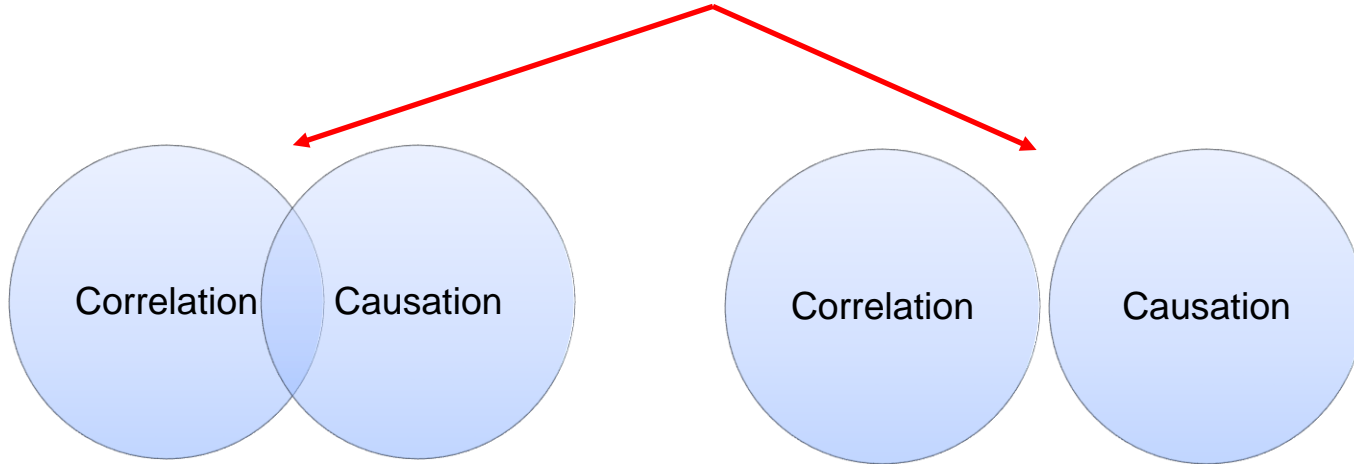
“..for conceptual and engineering breakthroughs that have made deep neural networks a critical component of computing.”

“Causality is very important for the next steps of progress of machine learning,”

Yoshua Bengio in an interview with IEEE Spectrum, 2020

# We have All Heard the Phrase

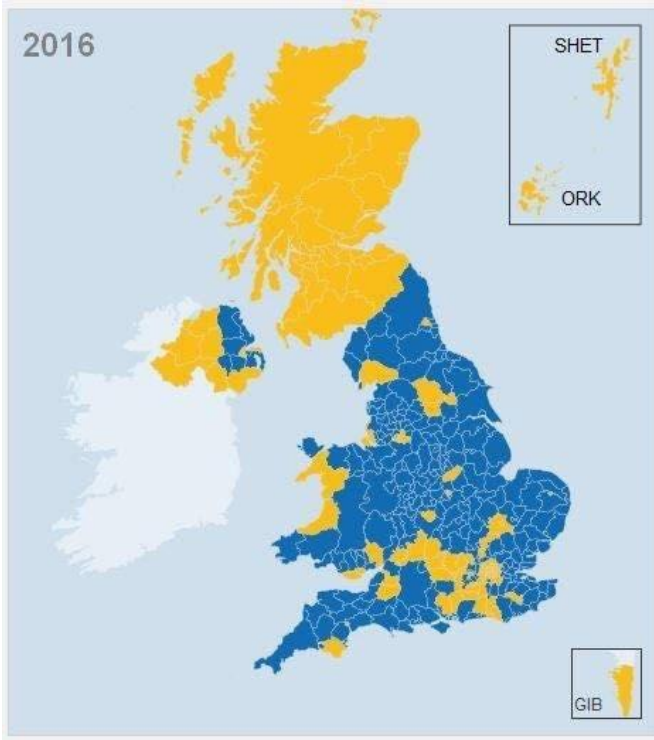
*“Correlation does not imply causation”*



Pic Credit: Wikipedia

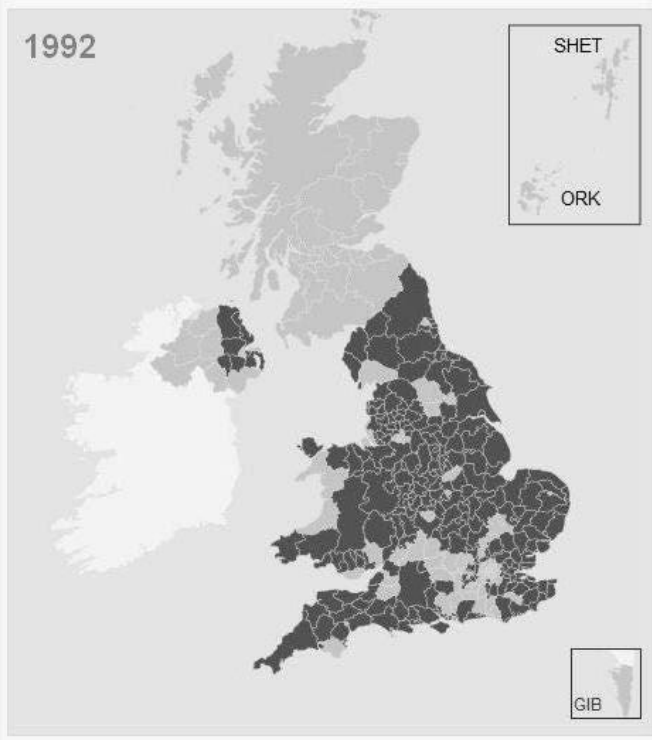


# Correlation $\cap$ Causality = $\emptyset$



Key:

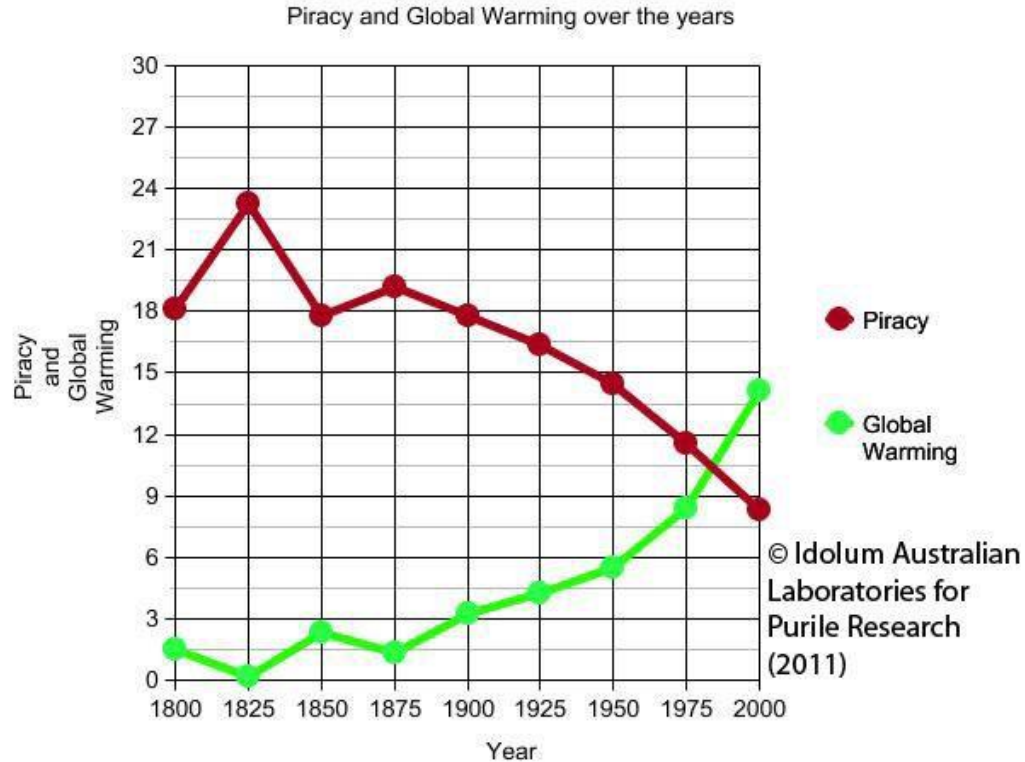
Majority leave    Majority remain



Key:

BSE-Areas    BSE-Free-Areas

# Correlation => Causality via a third factor





As of my last update in September 2021, there is no direct scientific evidence or research specifically focused on the effect of global warming on pirate ships. Global warming primarily refers to the long-term increase in Earth's average surface temperature due to human activities, such as the emission of greenhouse gases like carbon dioxide.



However, we can speculate on some potential indirect effects that global warming might have on pirate ships:

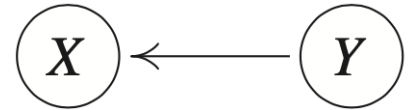
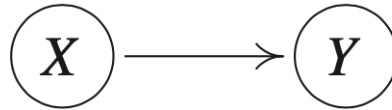
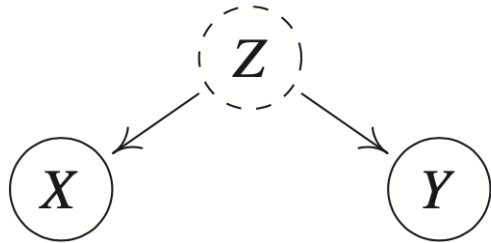
1. **Rising sea levels:** Global warming contributes to the melting of polar ice caps and glaciers, leading to rising sea levels. Higher sea levels can alter coastlines and navigational routes, making it challenging for pirate ships to access certain areas or ports.
2. **Changes in weather patterns:** Global warming can lead to shifts in weather patterns, including more intense storms, hurricanes, and cyclones. These extreme weather events can be dangerous for pirate ships at sea and may increase the risk of accidents or shipwrecks.
3. **Ocean acidification:** The increased concentration of carbon dioxide in the atmosphere not only causes global warming but also results in more CO<sub>2</sub> being absorbed by the oceans. This process leads to ocean acidification, which can have implications for marine life, including the plankton and other organisms that form the base of the marine food chain. Changes in marine ecosystems could indirectly impact pirate activity if their traditional hunting grounds are affected.
4. **Temperature changes:** While global warming generally leads to higher temperatures globally, localized effects can vary. Some regions may experience altered wind patterns and temperature shifts, which can influence the timing and strength of monsoons, trade winds, and other maritime conditions that pirates historically relied on for navigation.
5. **Economic and geopolitical impacts:** Global warming can disrupt economies and lead to resource scarcity in certain regions. These changes may influence trade routes and shift the focus of piracy to areas that were previously less affected.

It's essential to note that these are speculative effects, and any actual impact would likely depend on various factors such as the severity and pace of global warming, regional climate changes, and human responses to these challenges.

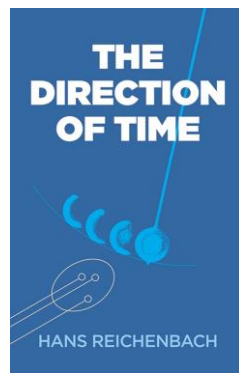
# Reichenbach's Common Cause Principle

## Defining Confounders

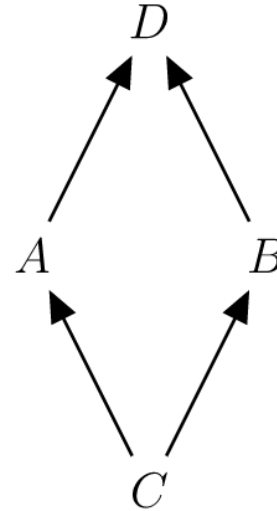
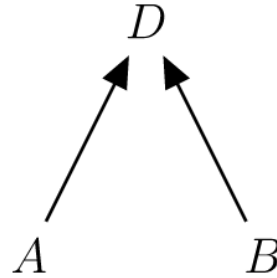
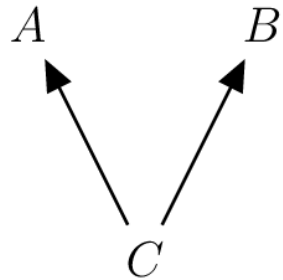
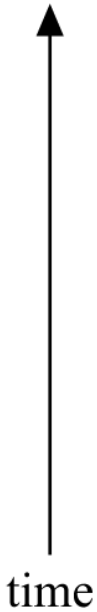
**Principle 1.** *If two random variables  $X$  and  $Y$  are statistically dependent ( $X \not\perp Y$ ), then there exists a third variable  $Z$  that causally influences both. (As a special case,  $Z$  may coincide with either  $X$  or  $Y$ .) Furthermore, this variable  $Z$  screens  $X$  and  $Y$  from each other in the sense that given  $Z$ , they become independent,  $X \perp Y \mid Z$ .*



Reichenbach's *Direction of Time* (1956)



# Reichenbach's Common Cause Principle



Conjunctive fork:

a) open to the future

b) open to the past

c) closed fork

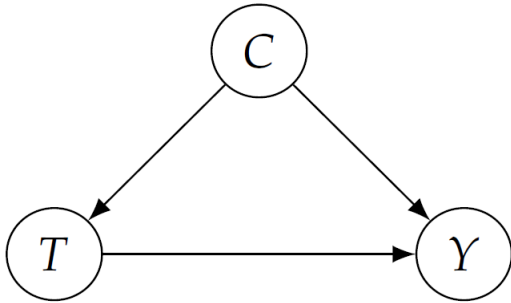
# Let's Illustrate Correlation does not imply causation: Simpson's Paradox

		Condition		
		Mild	Severe	Total
Treatment	A	15% (210/1400)	30% (30/100)	<b>16%</b> (240/1500)
	B	<b>10%</b> (5/50)	<b>20%</b> (100/500)	19% (105/550)

more effective treatment is completely dependent on the **causal structure** of the problem

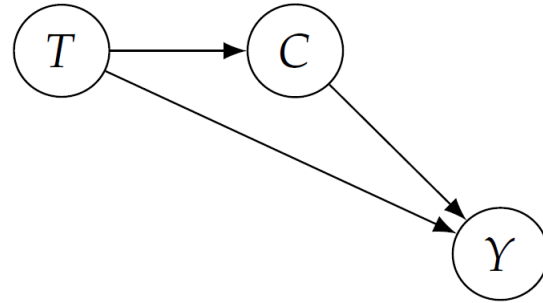
# Let's Illustrate Correlation does not imply causation : Simpson's Paradox

Scenario 1: Confounders



**Treatment A preferable**

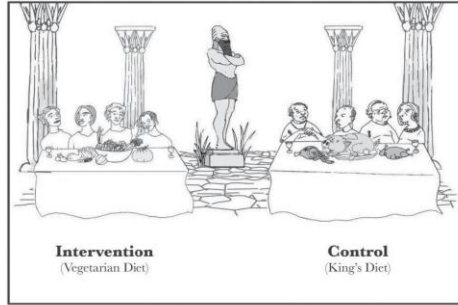
Scenario 2: Treatment causes condition



**Treatment B preferable**

# From Neyman-Rubin.....

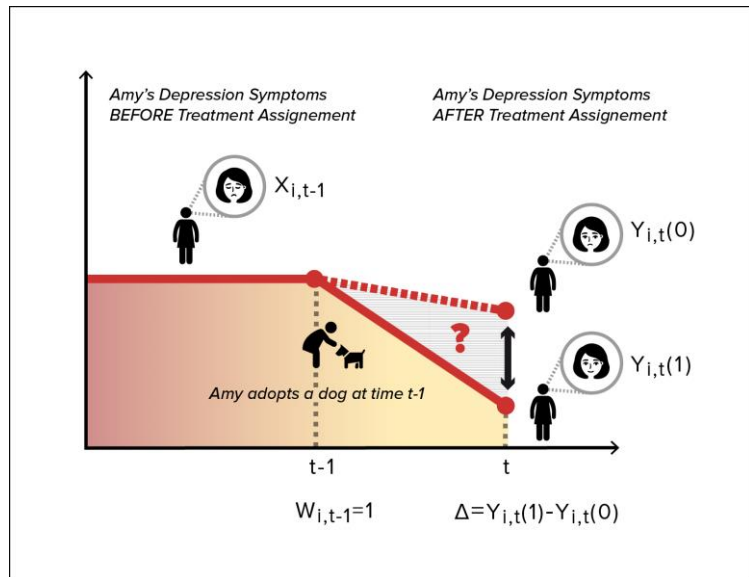
- Potential Outcome theory



The biblical story of Daniel, often cited as the first controlled experiment. Daniel (third from left?) realized that a proper comparison of two diets could only be made when they were given to two groups of similar individuals, chosen in advance. King Nebuchadnezzar (rear) was impressed with the results. (*Source:* Drawing by Dakota Harr.)



# Fundamental Problem of Causal Inference



Credit: Dominici et al., From Controlled to Undisciplined Data: Estimating Causal Effects in the Era of Data Science Using a Potential Outcome Framework

**Definition 1: Individual treatment effect**

The individual treatment effect,  $\delta_i$ , equals  $Y_i^1 - Y_i^0$

**Definition 3: Switching equation**

An individual's observed health outcomes,  $Y$ , is determined by treatment assignment,  $D_i$ , and corresponding potential outcomes:

$$Y_i = D_i Y_i^1 + (1 - D_i) Y_i^0$$

$$Y_i = \begin{cases} Y_i^1 & \text{if } D_i = 1 \\ Y_i^0 & \text{if } D_i = 0 \end{cases}$$

**Definition 2: Average treatment effect (ATE)**

The average treatment effect is the population average of all  $i$  individual treatment effects

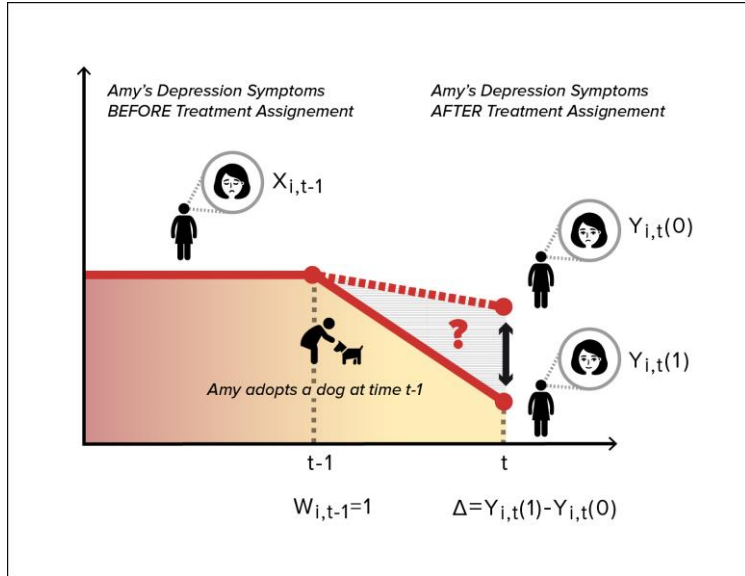
$$E[\delta_i] = E[Y_i^1 - Y_i^0]$$

$$= E[Y_i^1] - E[Y_i^0]$$

**What is the Apparent Problem?**

Credit: Scott Cunningham

# Fundamental Problem of Causal Inference



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The average treatment effect is the population average of all  $i$  individual treatment effects

$$E[\delta_i] = E[Y_i^1 - Y_i^0]$$

$$= E[Y_i^1] - E[Y_i^0]$$

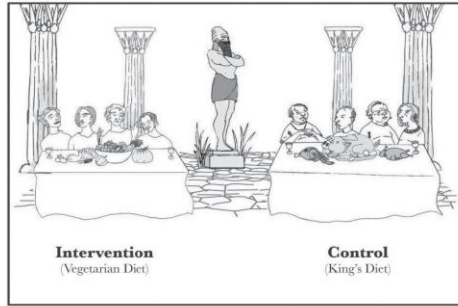
**Definition 4: Fundamental problem of causal inference**

It is impossible to observe both  $Y_i^1$  and  $Y_i^0$  for the same individual and so individual causal effects,  $\delta_i$ , are unknowable.

Credit: Scott Cunningham

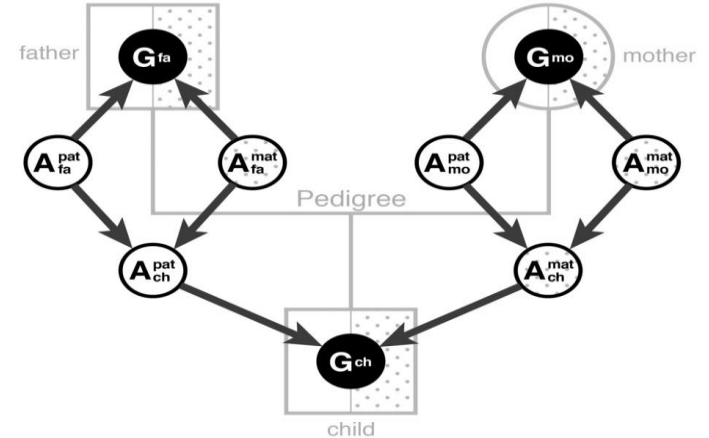
# From Neyman-Rubin to Pearl

- Potential Outcome theory to



The biblical story of Daniel, often cited as the first controlled experiment. Daniel (third from left?) realized that a proper comparison of two diets could only be made when they were given to two groups of similar individuals, chosen in advance. King Nebuchadnezzar (rear) was impressed with the results. (Source: Drawing by Dakota Harr.)

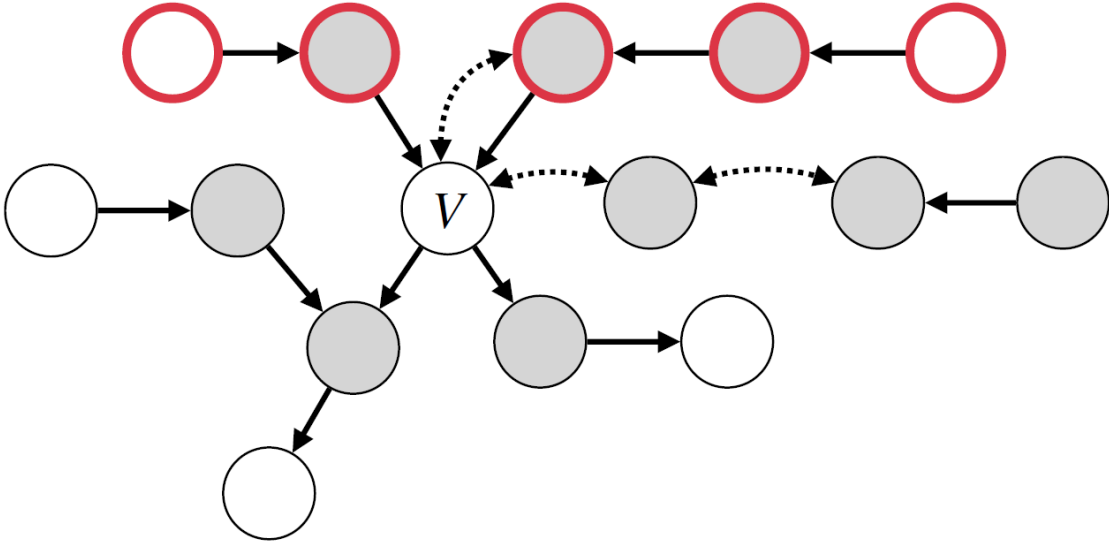
## Bayesian networks and DAG's



### Nodes of network:

- G** Genotype (observed in DNA test)
- A<sup>pat</sup>** Allele, paternal (unobservable)
- A<sup>mat</sup>** Allele, maternal (unobservable)

# Graphically Explaining Causes and Predictors



● Predictors == MB

○ Causes (direct/indirect)

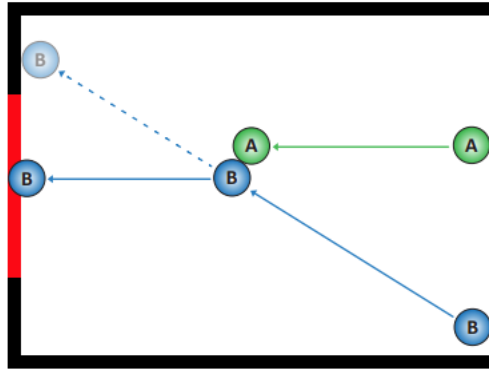
# Pearlian Causality

A success story

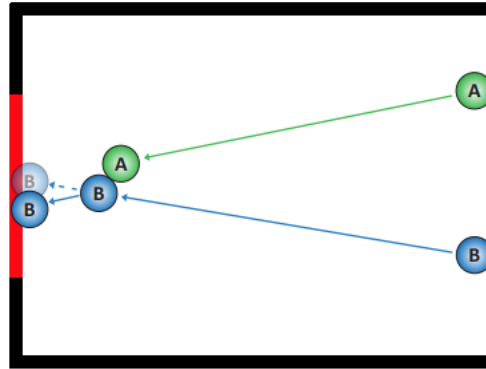
The formalization with most success in AI/ML so far.

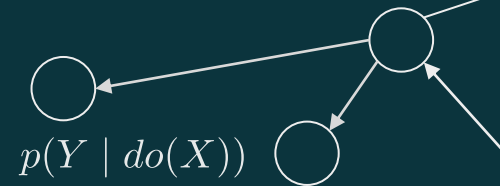
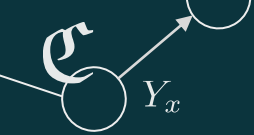
Works in Cognitive Science also in support of the key ideas in the formalism i.e., **humans reason counterfactually**.

(a) A caused B to go into the gate.



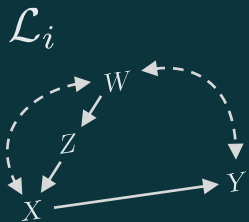
(b) A didn't cause B to go into the gate.





# 2 What?

Does Pearl's Causality look like?



*“Some tens of thousands of years ago, humans began to realize that certain things cause other things and that tinkering with the former can change the latter... From this discovery came organized societies, then towns and cities, and eventually the science and technology-based civilization we enjoy today. All because we asked a simple question: Why?” – in The Book of Why*

# Philosophical Insight

1. Dichotomy between “reality” & what we observe (data)
2. We only have access to data

e.g. J. Locke:

*“[when we observe data, we cannot] so much as guess, much less know, their manner of production”*



# Pearl's Solution

- Representation of Reality:

*Structural Causal Model (SCM)*

- Data of Reality (implied by SCM):

*Factual* information

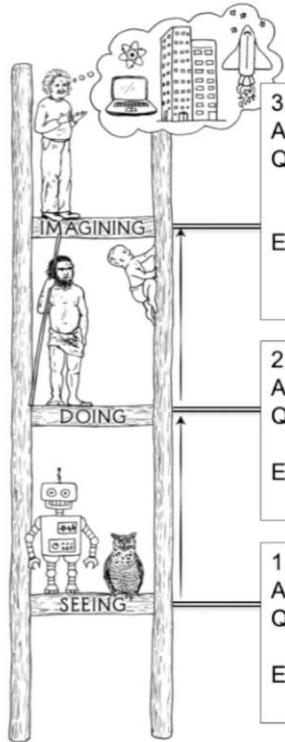
*Hypothetical* information

*Retrospective* information



Pearl's Causal Hierarchy (PCH)  
("Ladder of Causation")

# The Causal Hierarchy



## 3-LEVEL HIERARCHY

### 3. COUNTERFACTUALS

ACTIVITY: Imagining, Retrospection, Understanding

QUESTIONS: *What if I had done . . . ? Why?*

(Was it X that caused Y? What if X had not occurred? What if I had acted differently?)

EXAMPLES: Was it the aspirin that stopped my headache?

Would Kennedy be alive if Oswald had not killed him? What if I had not smoked the last 2 years?

### 2. INTERVENTION

ACTIVITY: Doing, Intervening

QUESTIONS: *What if I do . . . ? How?*

(What would Y be if I do X?)

EXAMPLES: If I take aspirin, will my headache be cured?

What if we ban cigarettes?

### 1. ASSOCIATION

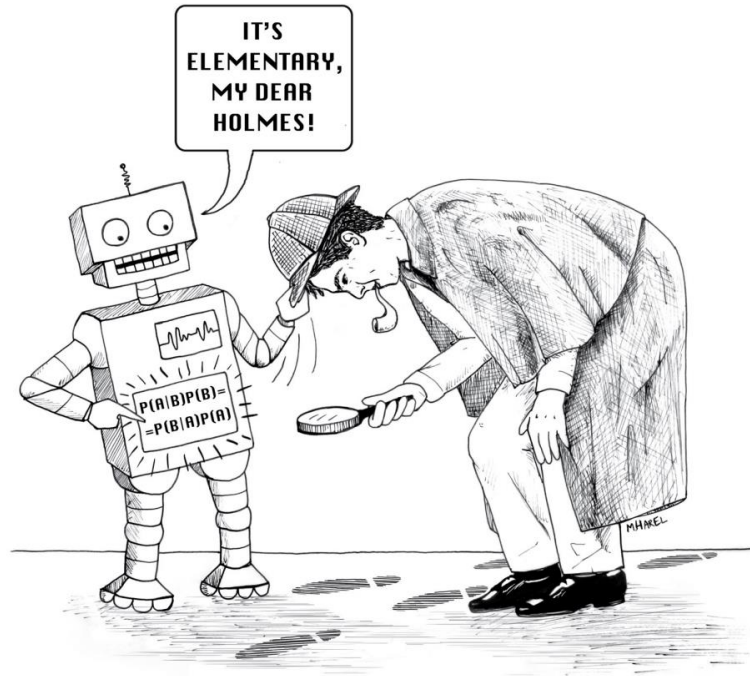
ACTIVITY: Seeing, Observing

QUESTIONS: *What if I see . . . ?*

(How would seeing X change my belief in Y?)

EXAMPLES: What does a symptom tell me about a disease?

What does a survey tell us about the election results?



Sherlock Holmes meets his modern counterpart, a robot equipped with a Bayesian network. In different ways both are tackling the question of how to infer causes from observations. The formula on the computer screen is Bayes's rule. (Source: Drawing by Maayan Harel.)

# Pearl Causal Ladder

## Level I

### 1. ASSOCIATION

**ACTIVITY:** Seeing, Observing

**QUESTIONS:** *What if I see ...?*  
(How are the variables related?  
How would seeing X change my belief in Y?)

**EXAMPLES:** What does a symptom tell me about a disease?  
What does a survey tell us about the  
election results?



# Pearl Causal Ladder

## Level II

### 2. INTERVENTION

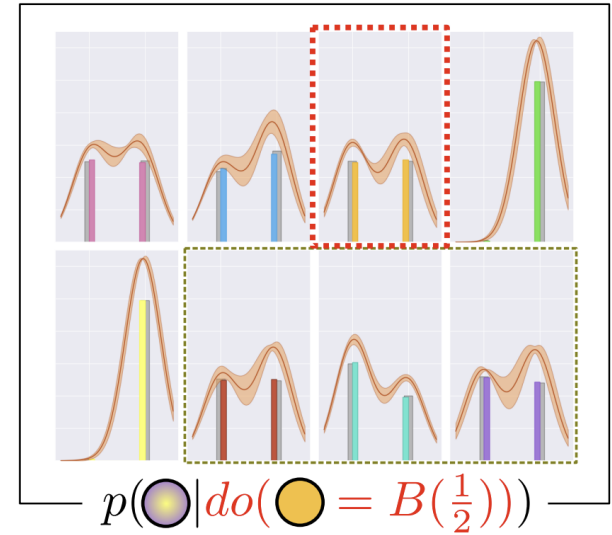
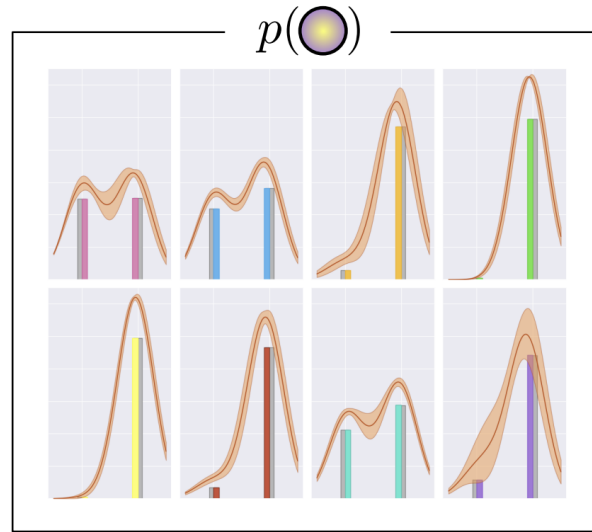
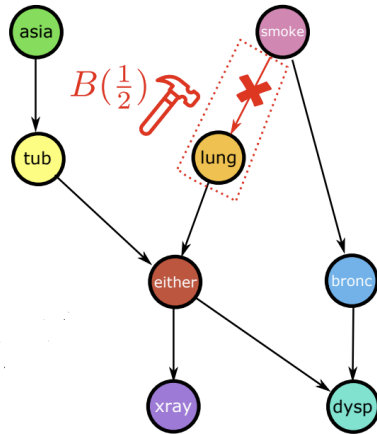
**ACTIVITY:** Doing, Intervening

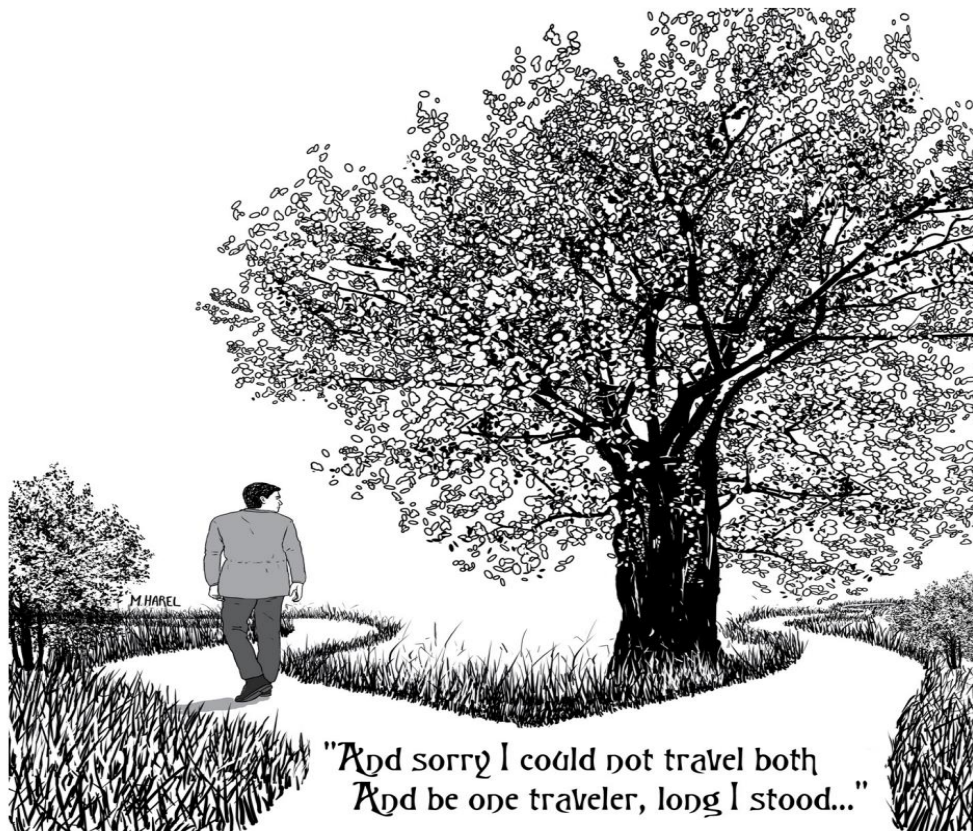
**QUESTIONS:** *What if I do ...? How?*  
(What would Y be if I do X?  
How can I make Y happen?)

**EXAMPLES:** If I take aspirin, will my headache be cured?  
What if we ban cigarettes?

# Pearl Causal Ladder

## Level II





"And sorry I could not travel both  
And be one traveler, long I stood..."

Robert Frost's famous lines show a poet's acute insight into counterfactuals. We cannot travel both roads, and yet our brains are equipped to judge what would have happened if we had taken the other path. Armed with this judgment, Frost ends the poem pleased with his choice, realizing that it "made all the difference." (Source:

Drawing by Maayan Harel.)



# Pearl Causal Ladder

## Level III

### 3. COUNTERFACTUALS

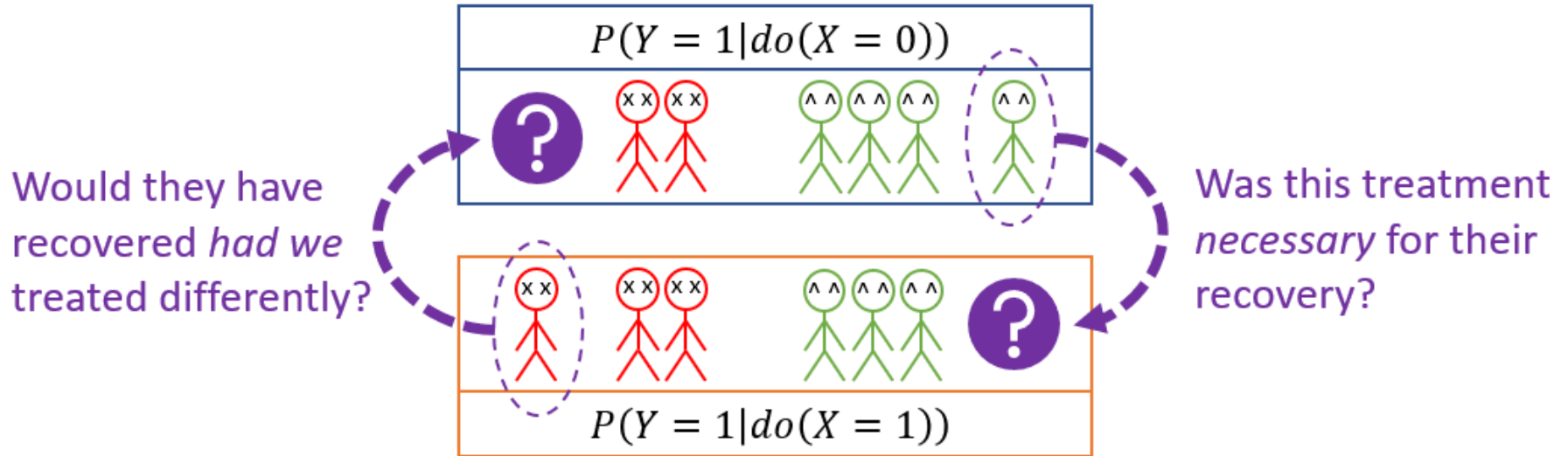
**ACTIVITY:** Imagining, Retrospection, Understanding

**QUESTIONS:** *What if I had done ...? Why?*  
(Was it X that caused Y? What if X had not occurred? What if I had acted differently?)

**EXAMPLES:** Was it the aspirin that stopped my headache?  
Would Kennedy be alive if Oswald had not killed him? What if I had not smoked for the last 2 years?

# Pearl Causal Ladder

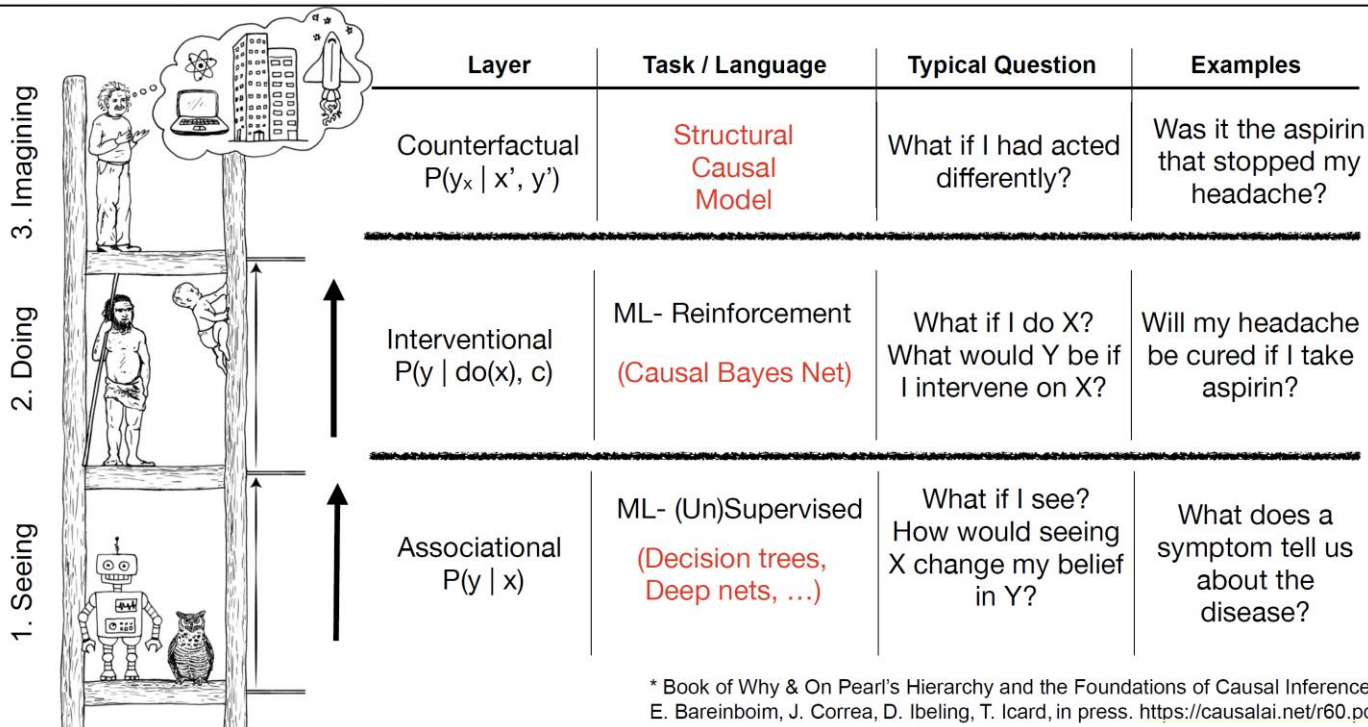
## Level III



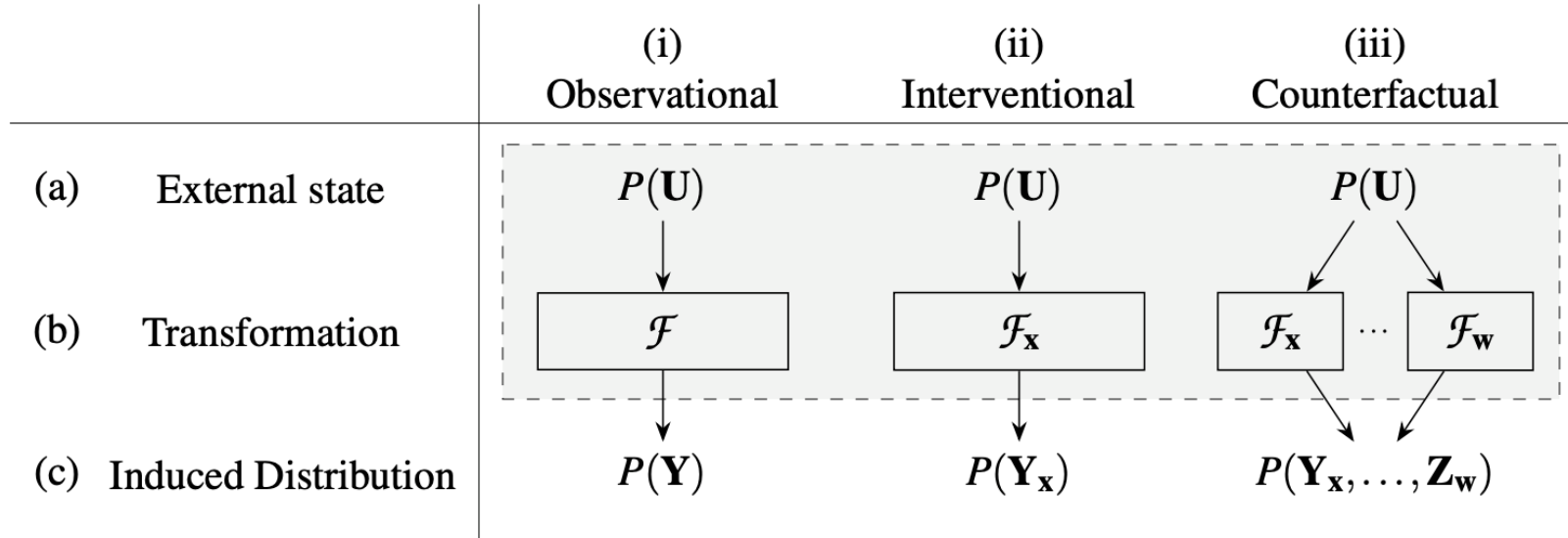
Credit: <https://forns.lmu.build/classes/spring-2019/cmsi-498/lecture-5T.html>

# Pearl's Hierarchy

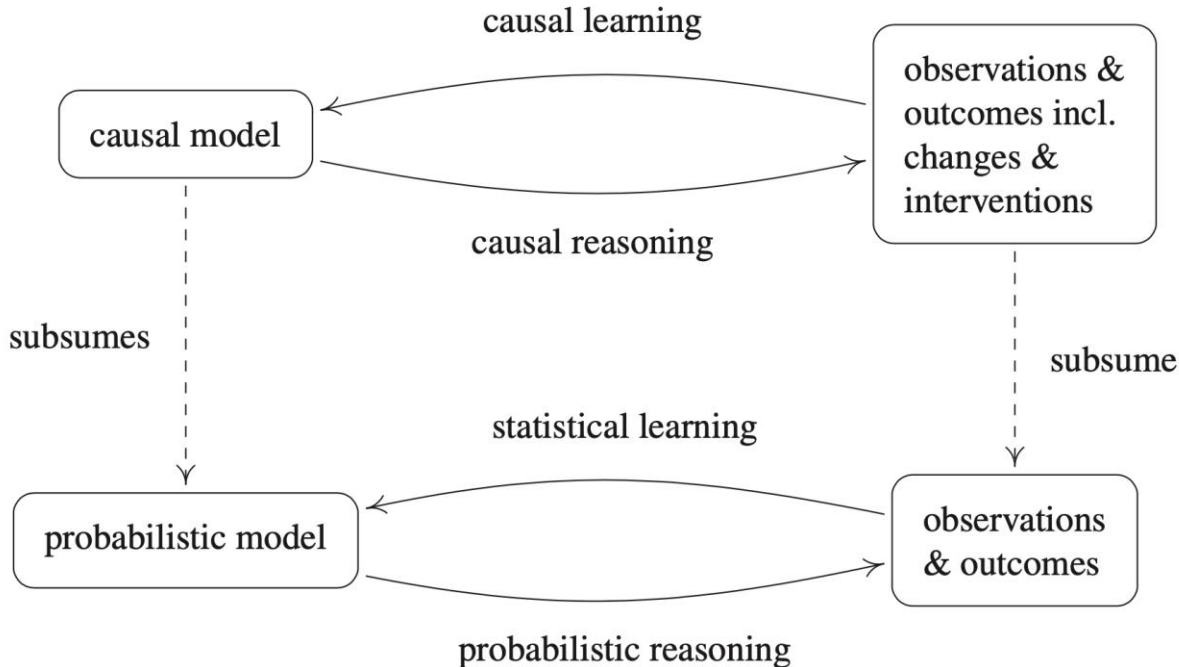
## Ladder of Causation



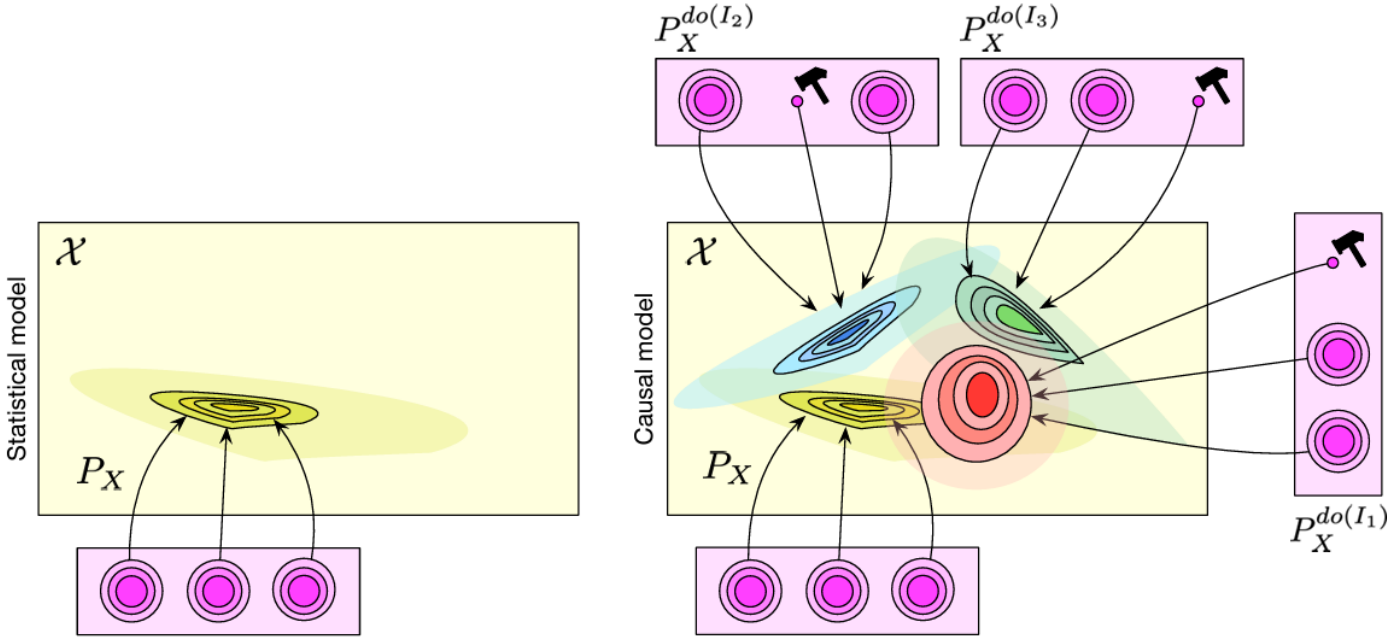
# Distinction Between the Rungs



# Causal versus Probabilistic Inference



# Causal versus Statistical Models



# Structural Causal Model (SCM)

## Definition

A structural causal model  $\mathcal{M}$  (or data generating model) is a tuple  $\langle \mathbf{V}, \mathbf{U}, \mathcal{F}, P_{\mathbf{U}} \rangle$ , where

$\mathbf{V}$  are endogenous variables

$\mathbf{U}$  are exogenous variables

$\mathcal{F}$  are functions determining  $\mathbf{V}$  i.e.,  $v_i = f_i(\mathbf{pa}_i, \mathbf{u}_i)$

$P_{\mathbf{U}}$  is the probability distribution over  $\mathbf{U}$ .

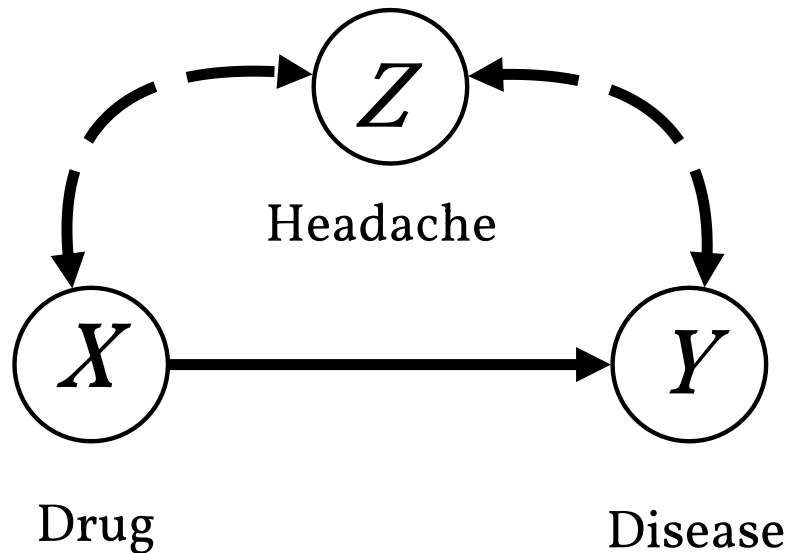
Assumption:  $\mathcal{M}$  is recursive i.e., there are no feedback (cyclic) mechanisms

# The Causal Graph

An induced property of the SCM

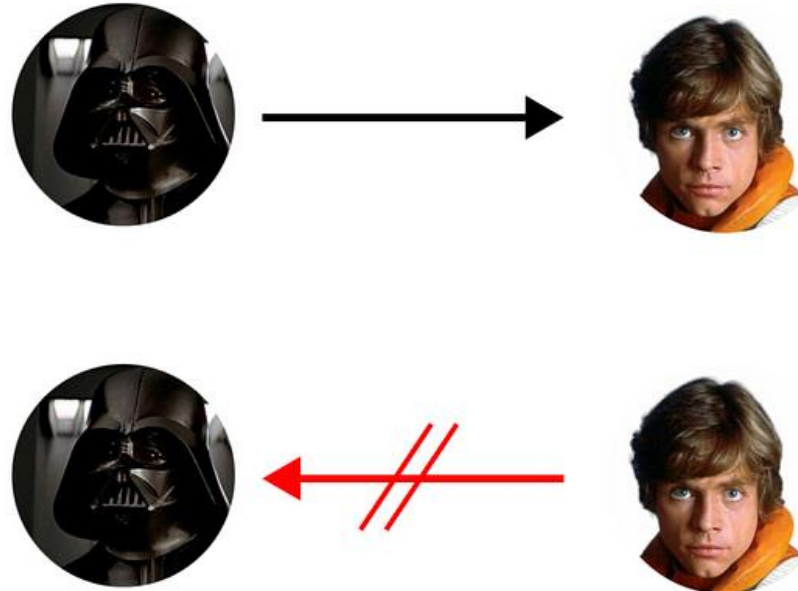
latent

$$\mathcal{F} = \begin{cases} X = f_X(U_X, U_{XZ}) \\ Y = f_Y(X, U_Y, U_{YZ}) \\ Z = f_Z(U_Z) \end{cases}$$





# A Causal Graph



Ancestor



Descendant



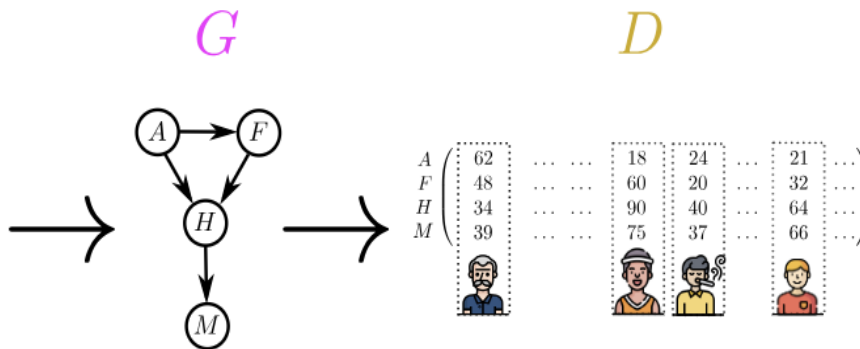
Descendant



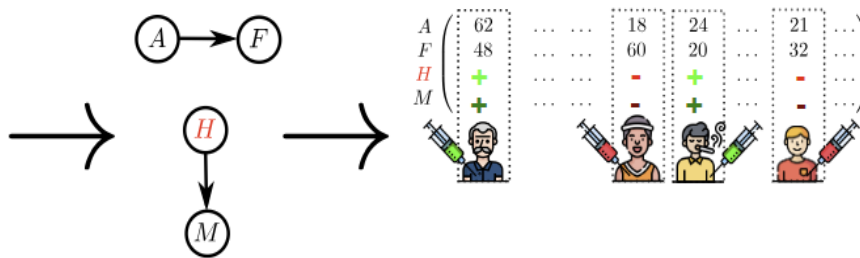
# The Causal Graph + Data

## Structural Causal Model

$$\begin{aligned}
 A &= U(0, 100) && \text{(A)ge} \\
 F &= \frac{1}{2}A + \mathcal{N}(10, 10) && \text{(F)ood Habits} \\
 H &= \frac{1}{100}(100 - A^2) + \frac{1}{2}F + \mathcal{N}(40, 30) && \text{(H)ealth} \\
 M &= \frac{1}{2}H + \mathcal{N}(20, 10) && \text{(M)obility}
 \end{aligned}$$

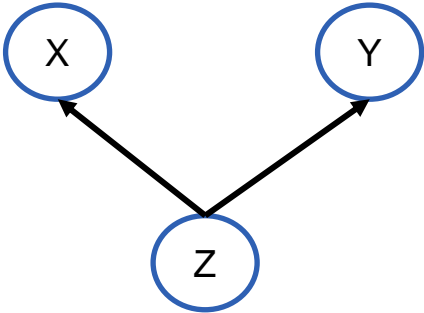
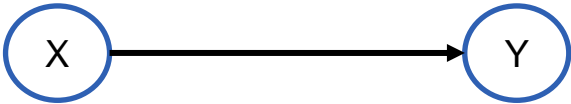


$$\begin{aligned}
 A &= U(0, 100) \\
 F &= \frac{1}{2}A + \mathcal{N}(10, 10) \\
 H &= U(0, 100) \\
 M &= \frac{1}{2}H + \mathcal{N}(20, 10)
 \end{aligned}$$

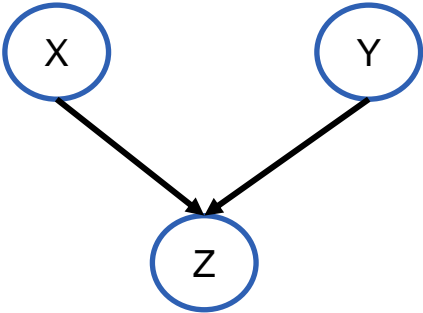


# The 3 Basic Graphs: “gifts from the gods”

Chain



Fork



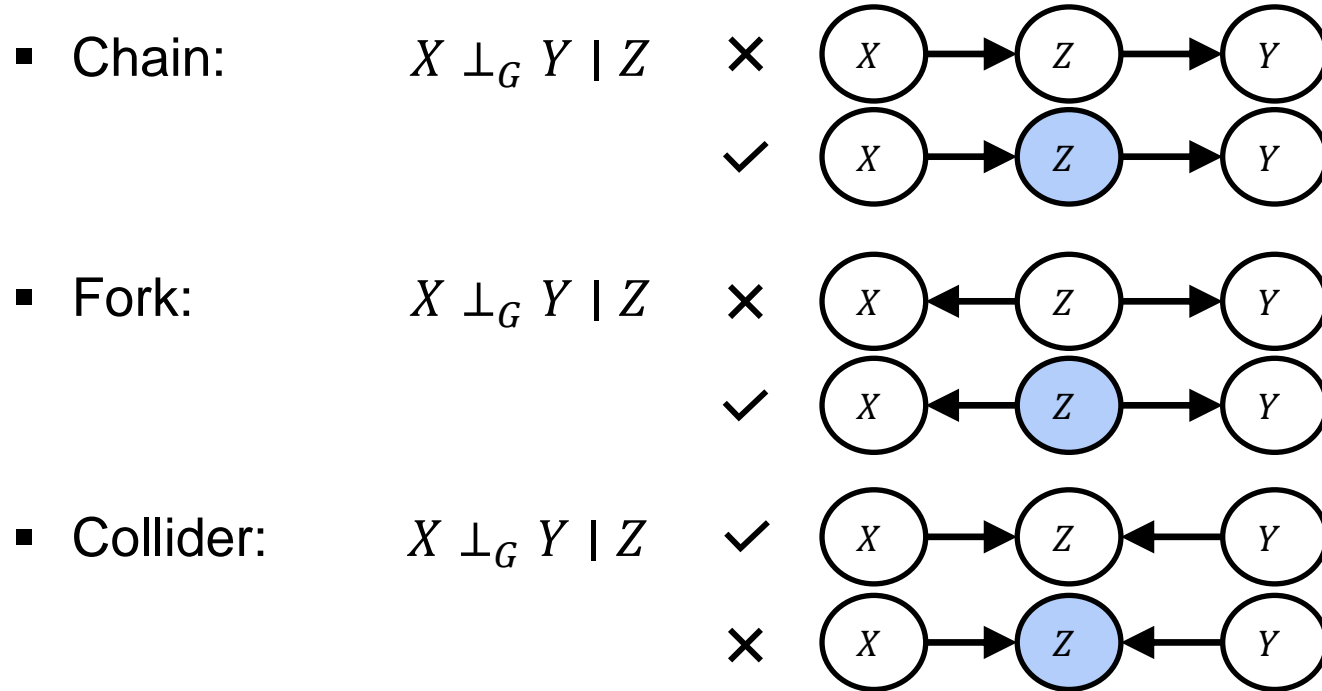
Collider

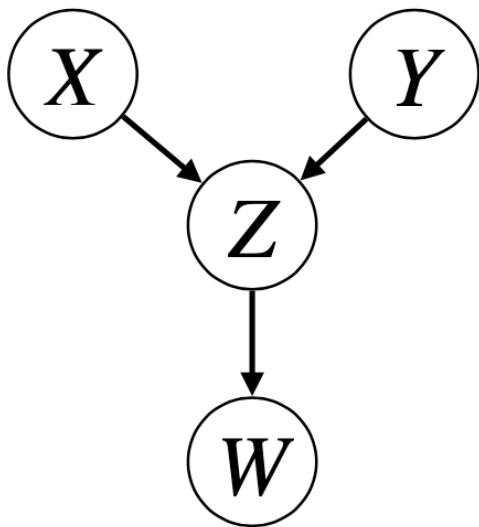
# How Graphs Encode Independence

- A path  $p$  is said to be d-separated by a set of nodes  $Z$  iff.
  1.  $p$  contains a chain  $i \rightarrow m \rightarrow j$  or a fork  $i \leftarrow m \rightarrow j$  such that the middle node  $m$  is in  $Z$ , or
  2.  $p$  contains a collider  $i \rightarrow m \leftarrow j$  such that the middle node  $m$  is not in  $Z$  and s.t. no descendant of  $m$  is in  $Z$

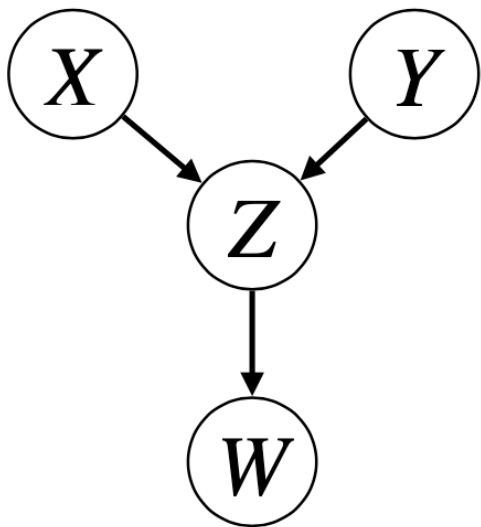
A set  $Z$  is said to d-separate  $X$  from  $Y$  if and only if  $Z$  blocks every path from a node in  $X$  to a node in  $Y$

# D-separation: Intuition





- $X$  is Diet  
 $Y$  is Physical Activity  
 $Z$  is Obesity  
 $W$  is Risk of Heart Disease
- Independences  $I(G)$ :  
 $X \perp_G W \mid Z,$   
 $Y \perp_G W \mid Z, \quad X \perp_G Y$



- For example, knowing that someone has a good diet but are obese let's us conclude that that someone lacks physical activity (up to correctness of  $G$ )



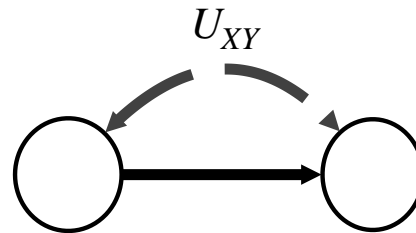
# Graphical Representation of an SCM

Structural Causal Model  
(SCM)

Graphical Causal Model  
(Causal Diagram)

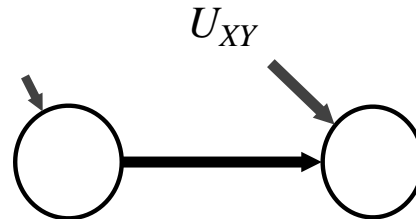
Observational

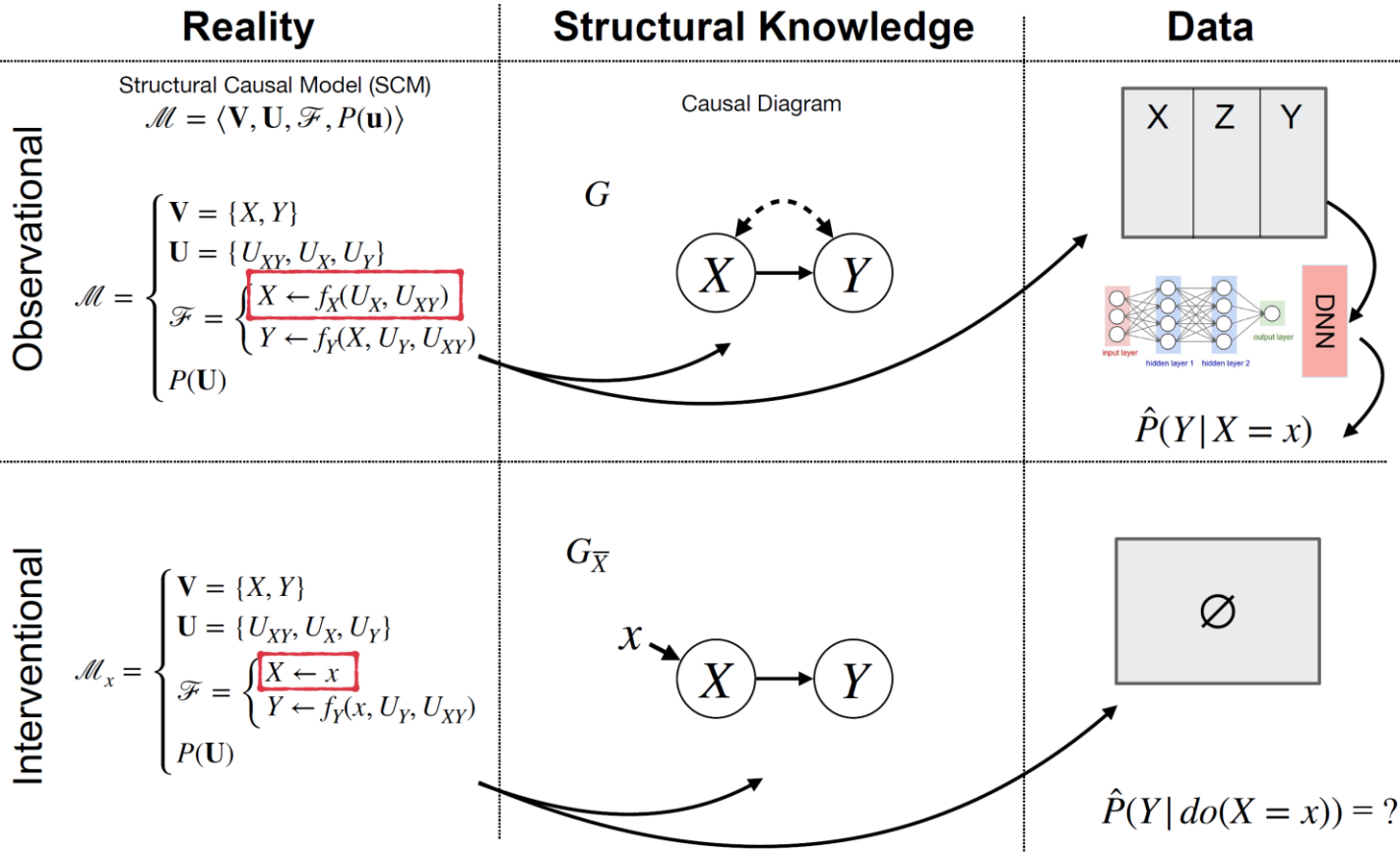
$$\mathcal{M} = \begin{cases} \mathbf{V} = \{X, Y\} \\ \mathbf{U} = \{U_{XY}, U_X, U_Y\} \\ \mathcal{F} = \begin{cases} X = f_X(U_X, U_{XY}) \\ Y = f_Y(X, U_Y, U_{XY}) \end{cases} \\ P(\mathbf{U}) \end{cases}$$



Interventional  
 $do(X = x)$

$$\mathcal{M} = \begin{cases} \mathbf{V} = \{X, Y\} \\ \mathbf{U} = \{U_{XY}, U_X, U_Y\} \\ \mathcal{F} = \begin{cases} X = x \\ Y = f_Y(x, U_Y, U_{XY}) \end{cases} \\ P(\mathbf{U}) \end{cases}$$

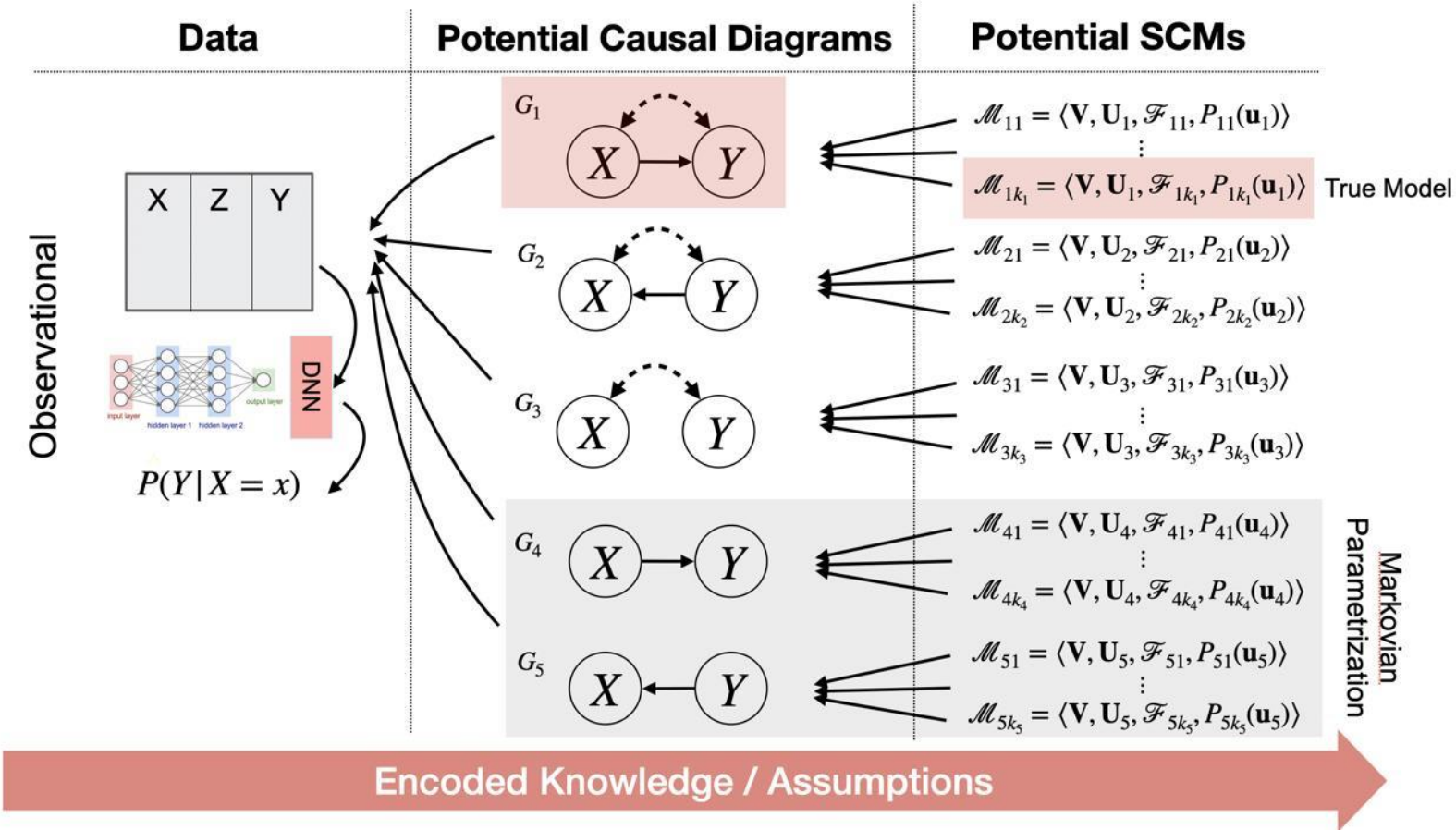


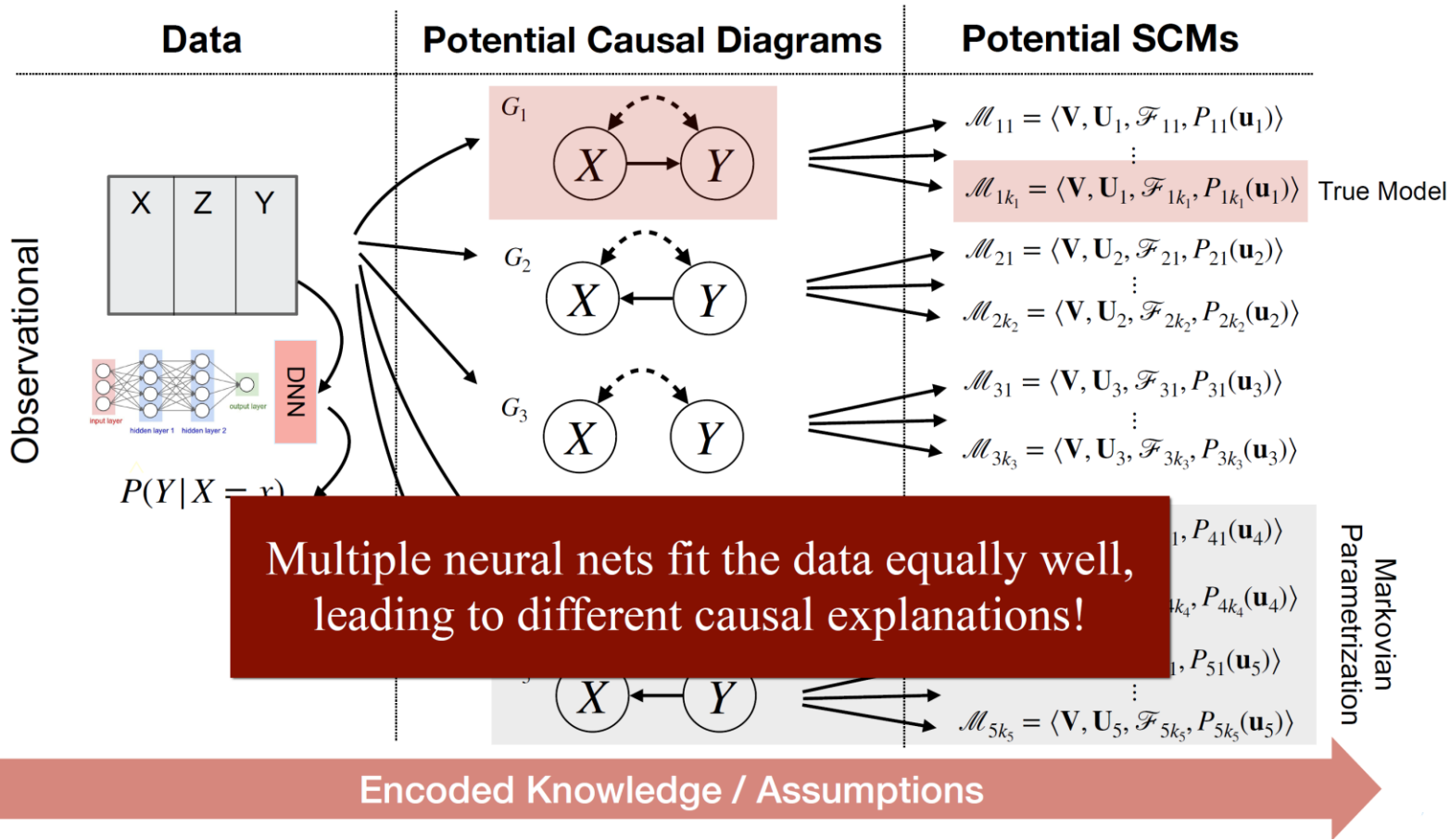


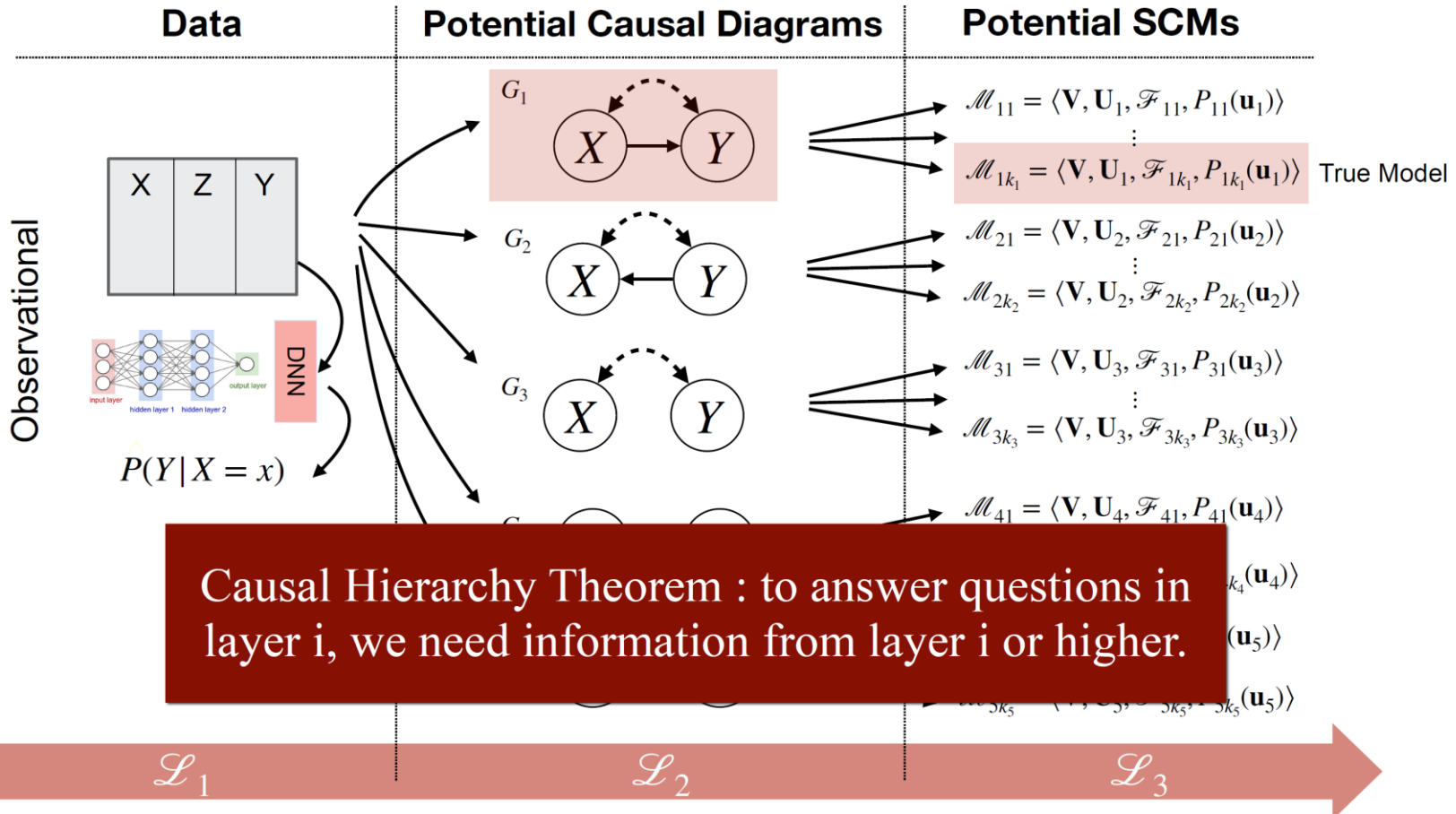
Seeing



Doing





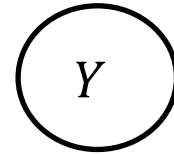
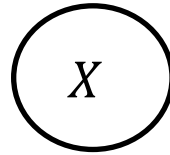


**Causal Hierarchy Theorem : to answer questions in layer i, we need information from layer i or higher.**

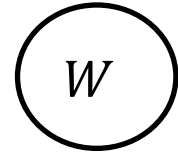
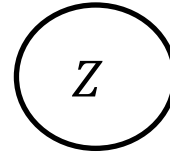


# Working with DAGs is Hard

- Number of nodes is 4



- Number of possible DAGs is **543**



# Super-Exponential Growth

- The number of possible DAGs depending on the number

$d$  of nodes:

$d$	Number of DAGs with $d$ nodes
1	1
2	3
3	25
4	543
5	29281
6	3781503
7	1138779265
8	783702329343
9	1213442454842881
10	4175098976430598143
11	31603459396418917607425
12	521939651343829405020504063
13	18676600744432035186664816926721
14	1439428141044398334941790719839535103
15	237725265553410354992180218286376719253505
16	83756670773733320287699303047996412235223138303
17	62707921196923889899446452602494921906963551482675201
18	99421195322159515895228914592354524516555026878588305014783
19	332771901227107591736177573311261125883583076258421902583546773505

*The length of the numbers grows faster than any linear term*

# Counterfactuals

A 3-step procedure

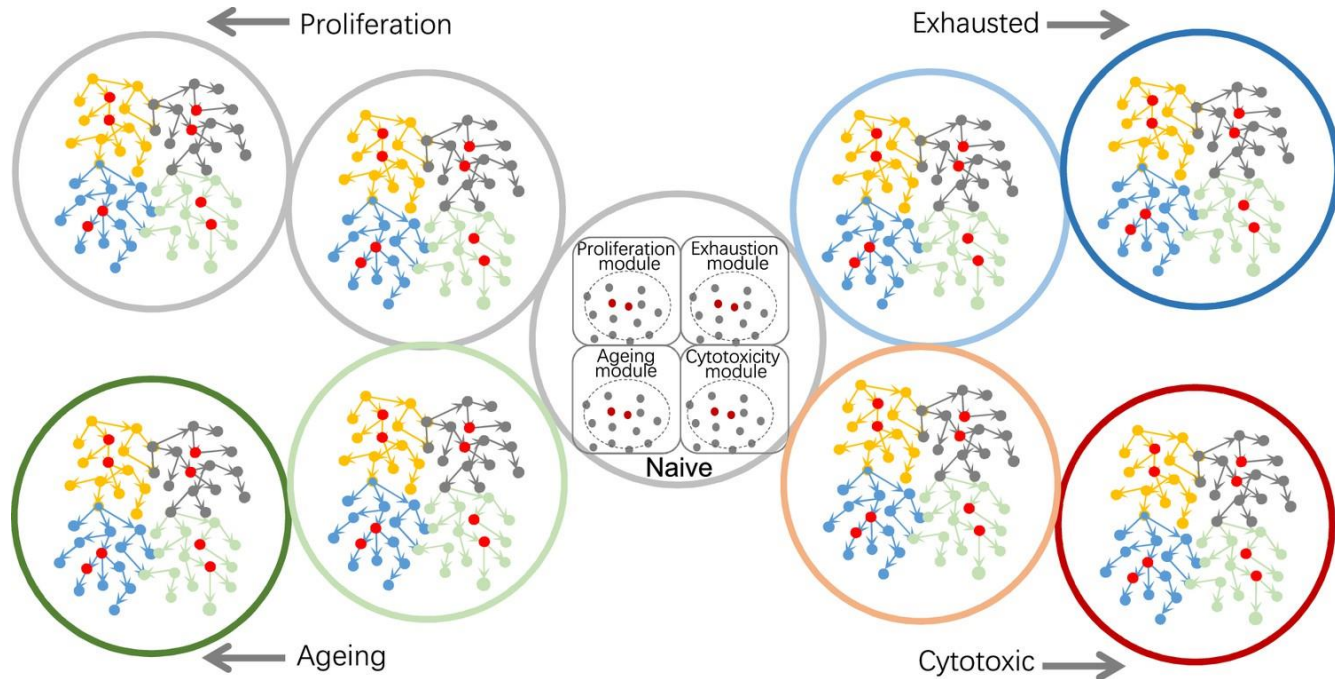
Abduction : Update belief in exogeneous variables given evidence

Action : Change equations accordingly,  $do(X = x)$

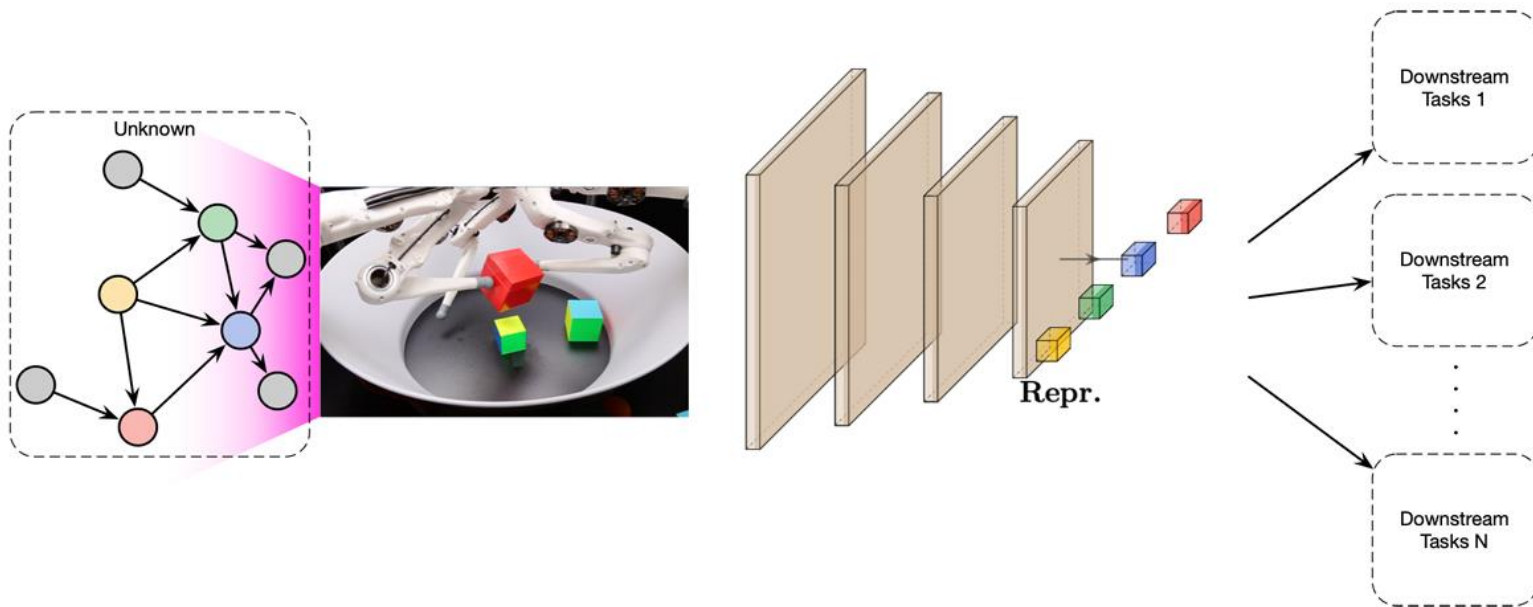
Prediction : Look at variable of interest  $P(Y = y)$



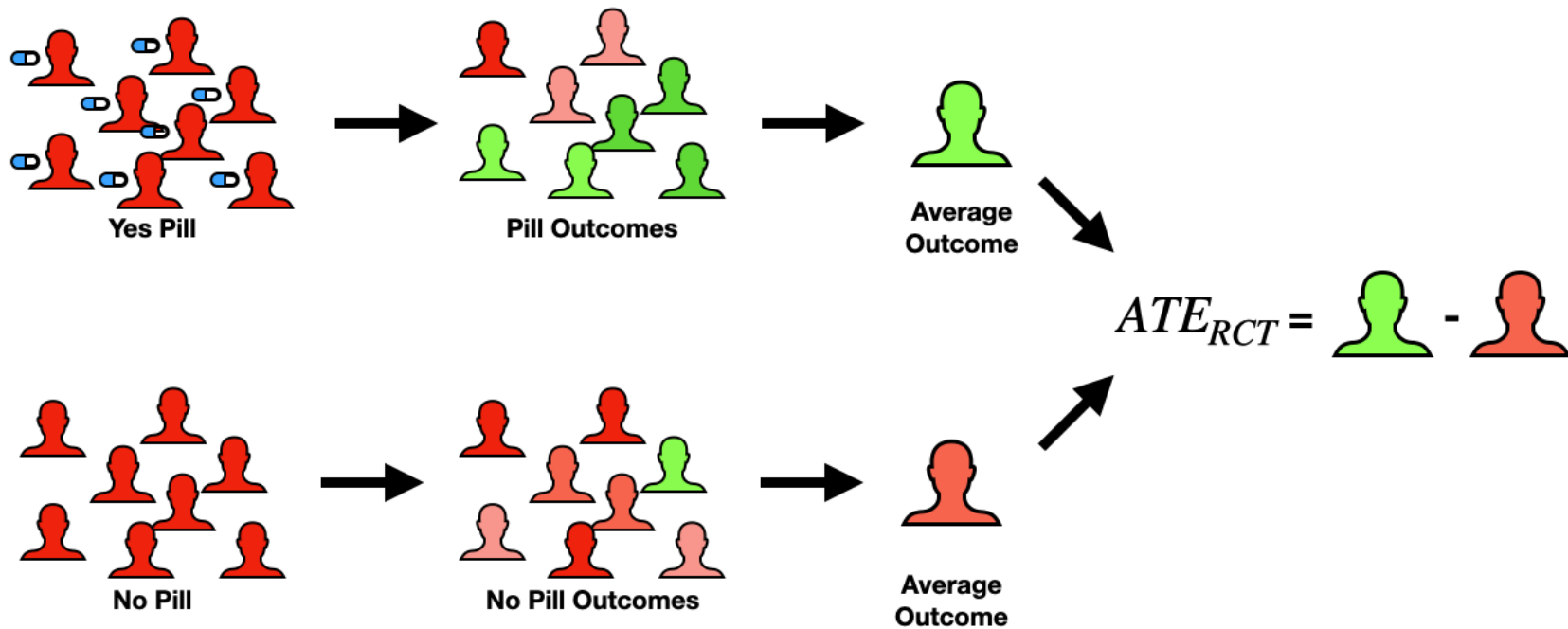
# Problems to be solved



# Problems to be solved

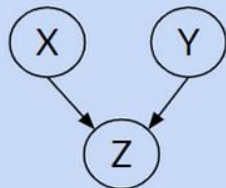


# Problems to be solved



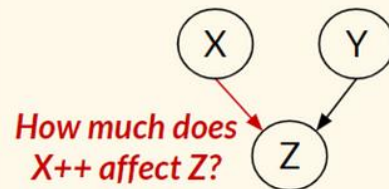
# Problems to be solved

Assume the variables and causal graph.



## Causal Effect Estimation

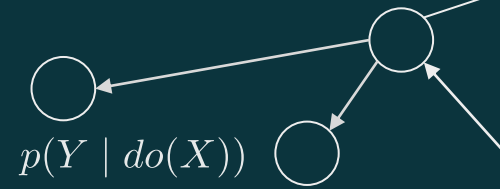
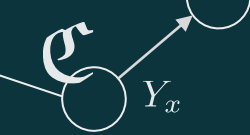
3. By how much?



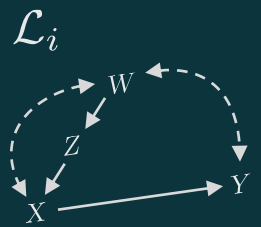
4. Full understanding

$$Z = f(X, Y, \sigma)$$

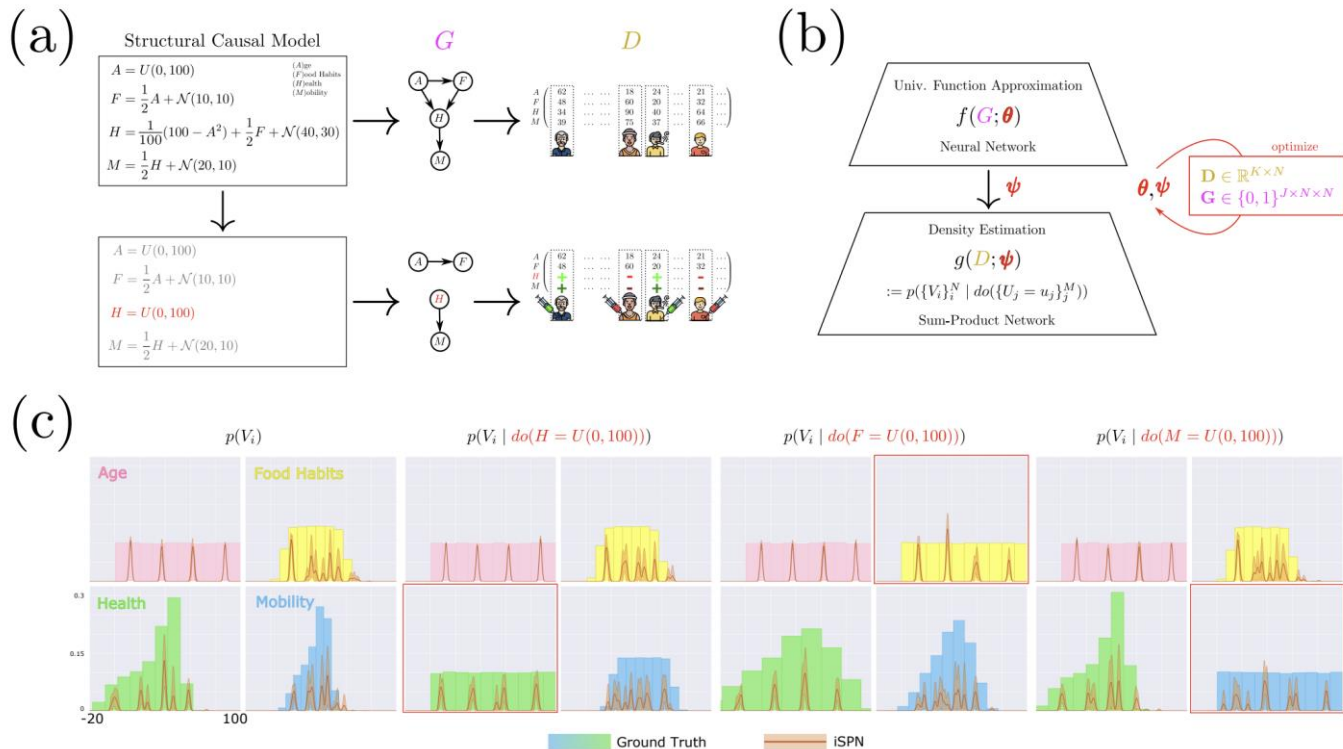
Human civilization advances 🚀.



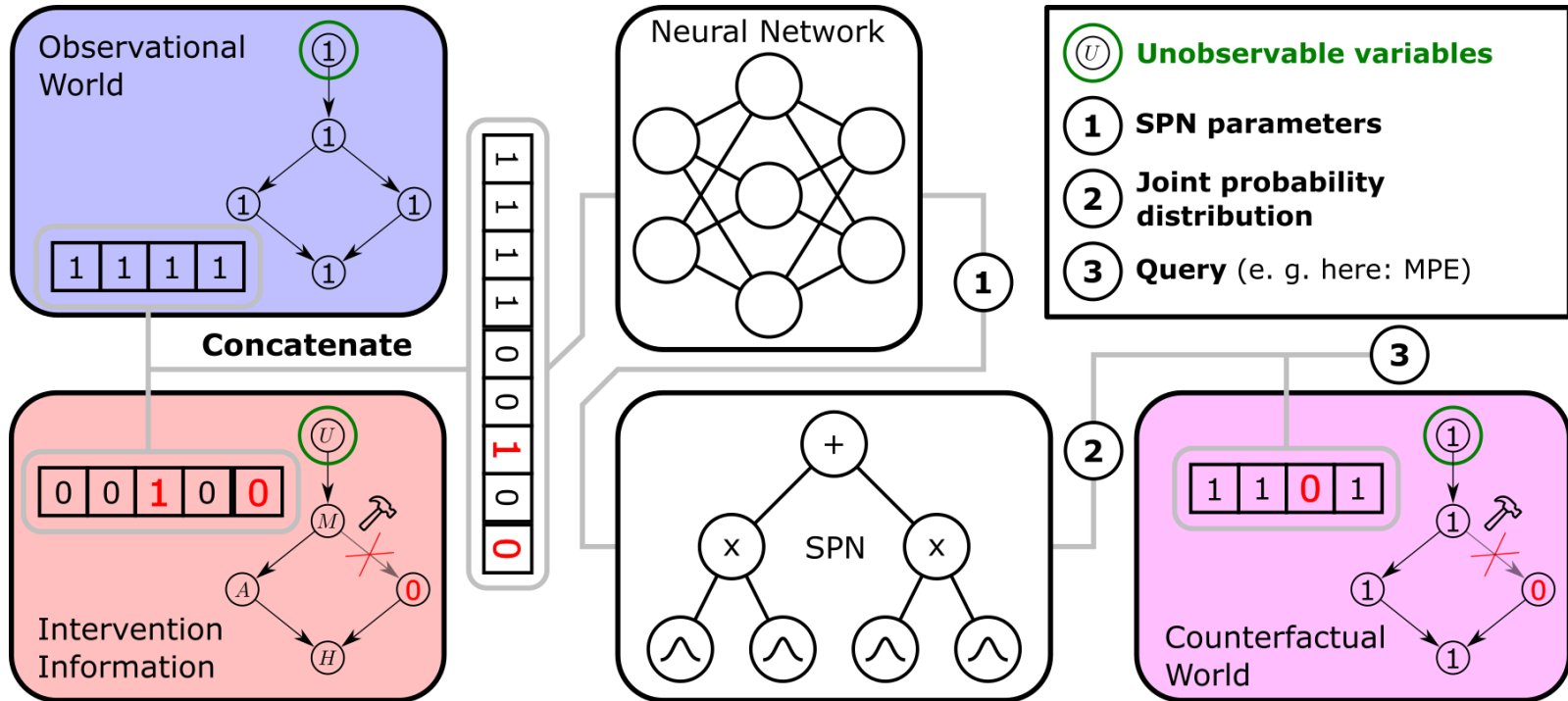
# 3 Machine Learning for Causality: A Flavour



# Probabilistic Circuits + Causality

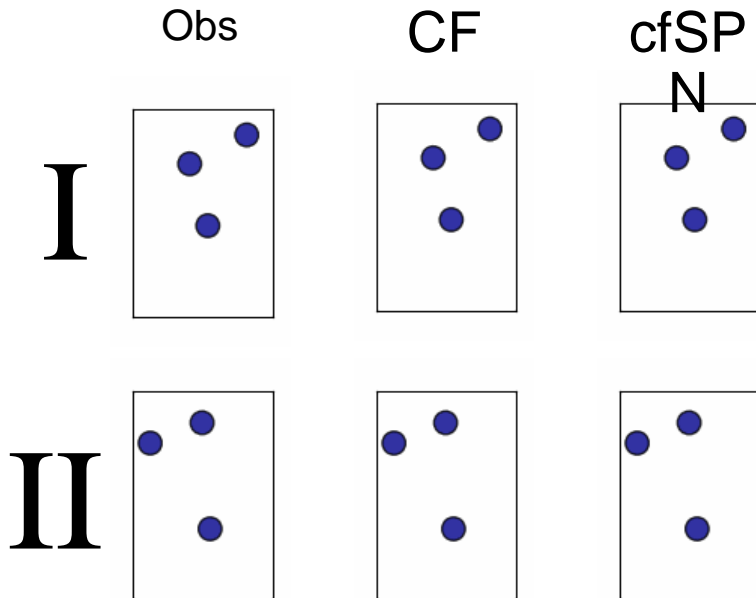


# Counterfactual Sum-Product Networks



# Experiment: Particle Collision

- A difficult problem: Particle simulation with gravity and collisions
- Goal: cfSPN prediction should match true counterfactual simulation (CF)
- I: Move the bottom particle to the right after some timesteps
- II: Change the velocity of the top particle to slightly upwards at the start

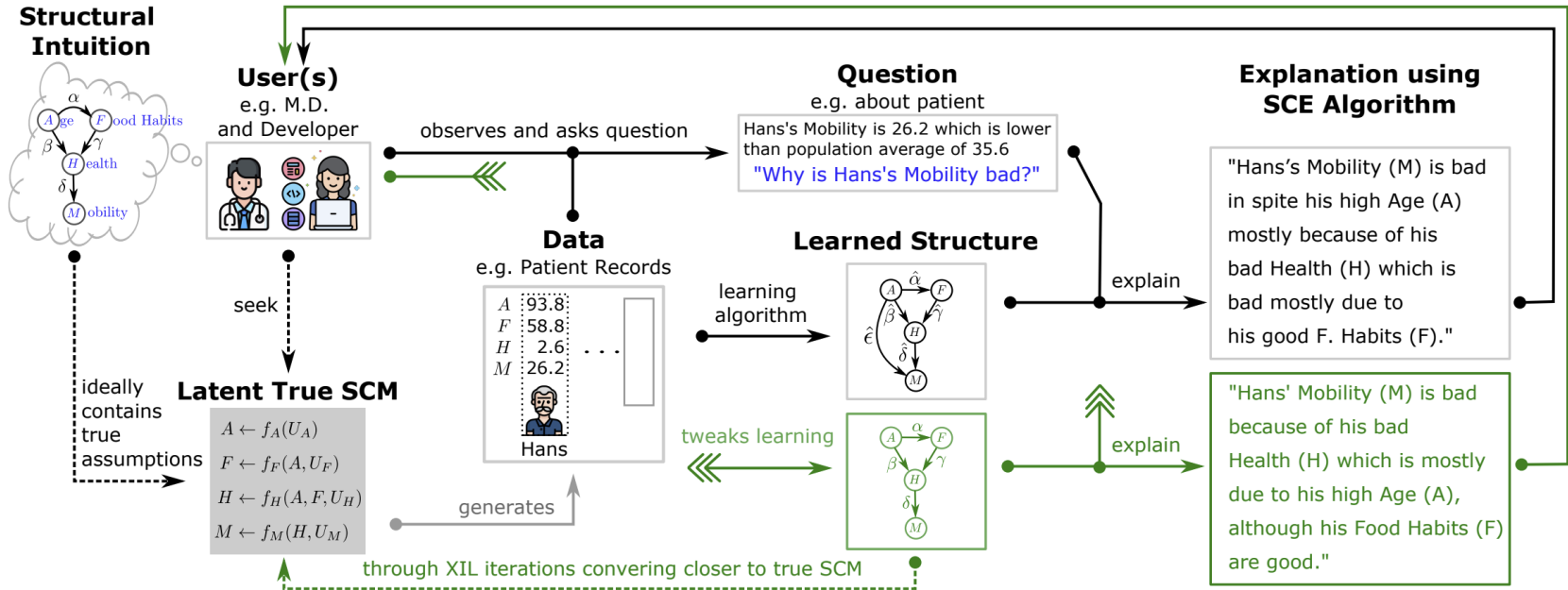


Based on the code repository for particle simulation:  
[https://github.com/ineporozhnii/particles\\_in\\_a\\_box](https://github.com/ineporozhnii/particles_in_a_box)



# Logic + Causality = Explanations

feedback to user, XIL loop closes and user suggests correction /  
after iteration(s) user is satisfied, trust increases, model performance increases



# Free Code Libraries

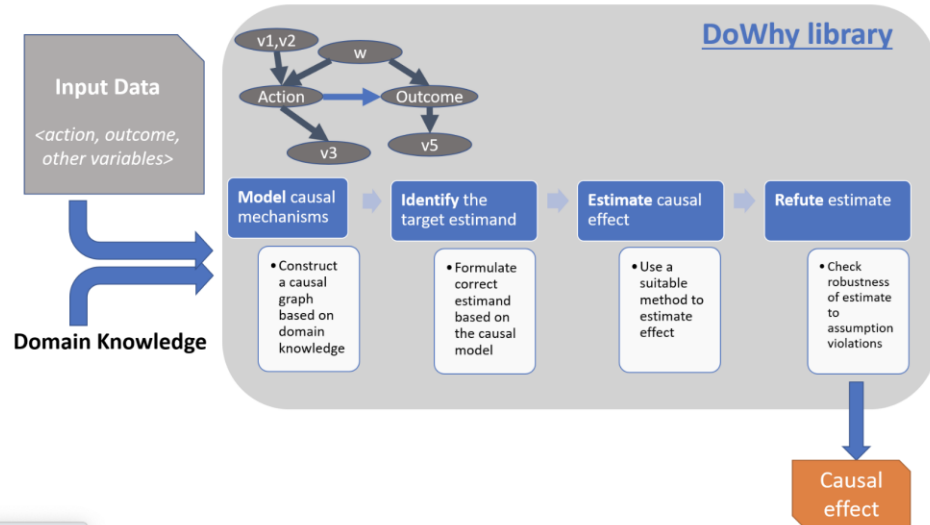
Do it for you

🔗 [DoWhy | An end-to-end library for causal inference](#)

Introducing DoWhy and the 4 steps of causal inference | [Microsoft Research Blog](#) | [Video Tutorial](#) | [Arxiv Paper](#) | [Arxiv Paper \(GCM-extension\)](#) | [Slides](#)

Read the [docs](#) | Try it online! [launch](#) [binder](#)

**Case Studies using DoWhy:** [Hotel booking cancellations](#) | [Effect of customer loyalty programs](#) | [Optimizing article headlines](#) | [Effect of home visits on infant health \(IHDP\)](#) | [Causes of customer churn/attrition](#)

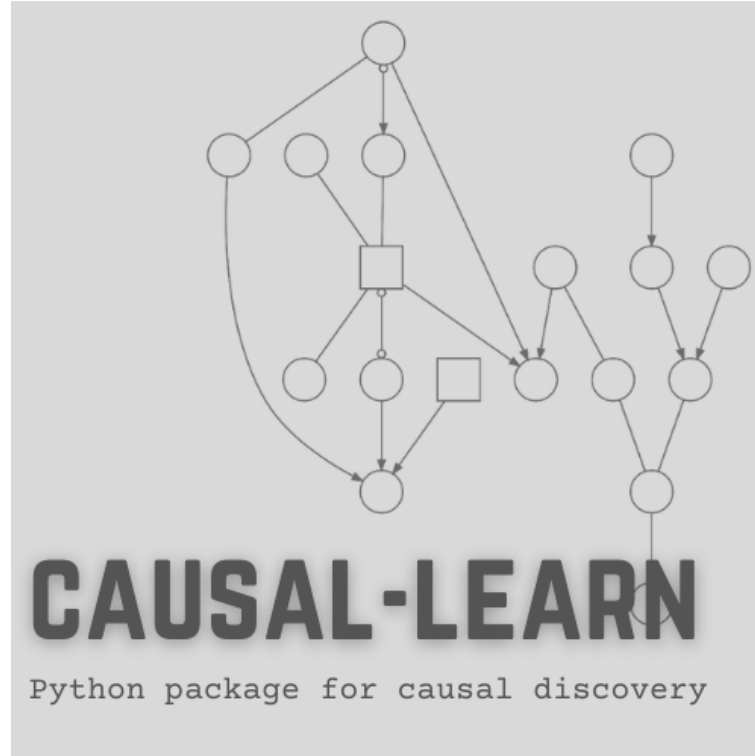


m/abs/2206.06821

DoWhy, <https://github.com/py-why/dowhy>

# Free Code Libraries

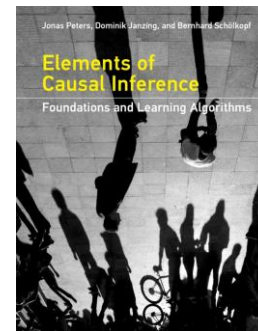
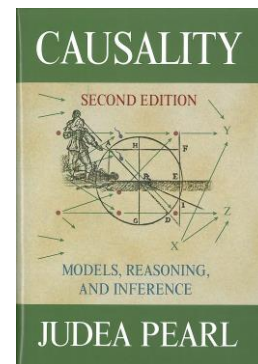
Do it for you



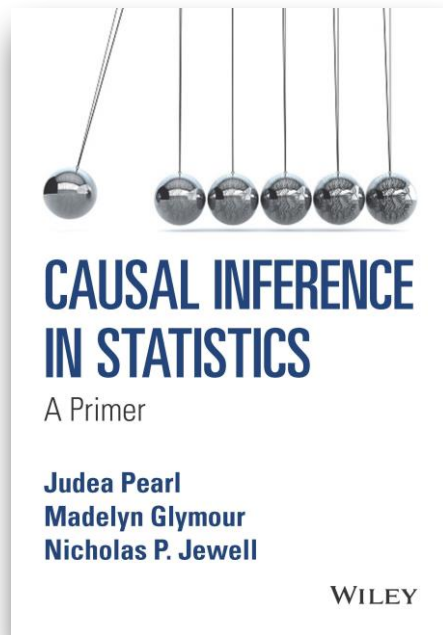
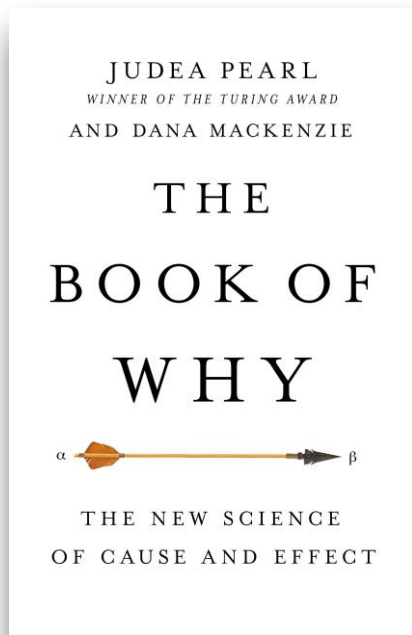
DoWhy, <https://github.com/py-why/causal-learn>

# Pointers to Causal Inference References

- ✓  Judea Pearl, “**Causality**”, Cambridge University Press, 2009.
- ✓  Peters et al., “**Elements of Causal Inference**”, MIT Press, 2017.
  - Elias Bareinboim Lecture “**Causal Data Science**”, 2019.  
<https://www.youtube.com/watch?v=dUsokjG4DHC>
- ✓  Brady Neal’s Free Online Course “**Introduction to Causal Inference**”, 2020.  
<https://www.bradyneal.com/causal-inference-course>
- Jonas Peters Lecture Series “**Causality**”, 2017.  
<https://www.youtube.com/watch?v=zvrcyqcN9wo>



# Causality Theory by Judea Pearl



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■  
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Judea Pearl	UCLA	?	US	Rutgers, Technion, New
Wesley Salmon	UCLA	Hans Reichenbach	US	?
Hans Reichenbach	UCLA	Paul Hensel, Max Noeth	US	Berlin, Istanbul, Erlange
<b>John Hopkins</b>				
Ilya Shpitser	John Hopkins		US	UCLA, Judea Pearl
<b>Oregon State University</b>				
Karthika Mohan	Oregon State University	Judea Pearl	US	
<b>CMU</b>				
Kun Zhang	CMU		Pittsburgh, US	MPI Tübingen
Clark Glymour	CMU	Wesley Salmon	Pittsburgh, US	
Peter Spirtes	CMU		Pittsburgh, US	
<b>ETH Zürich</b>				
Peter Bühlmann	ETH		Zürich	?
Marloes Maathuis	ETH		Zürich	?
Nicolai Meinshausen	ETH			
<b>LMU Munich</b>				
Stephan Hartmann	LMU		Munich, Germany	
<b>MPI Tübingen</b>				
Bernhard Schölkopf	MPI Tübingen	Vladimir Vapnik	Tübingen, Germ	TU Berlin
Ulrike von Luxburg	MPI Tübingen		Tübingen, Germany	
Michel Besserve				



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Name	Institution	Superior	Location	Previous Positions
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John				Managers, Tech Inc., Tech
Or				CSA, P, E, S, R
CA				
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U				
W				

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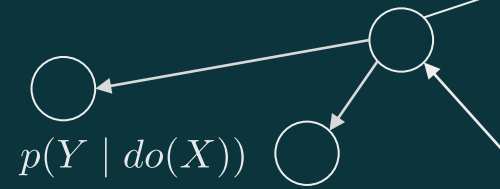
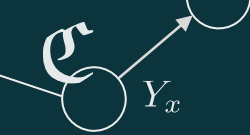


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Genealogy of Causality				
Name	Current Institution	Previous Institutions	Current Position	Previous Positions
<b>UCLA</b>				
Judea Pearl				Rutgers, Technion, New
Wesley Salmon	UCLA	Hans Reichenbach	US	?
Hans Reichenbach	UCLA	Paul Hensel, Max Noeth	US	Berlin, Istanbul, Erlange
<b>John Hopkins</b>				
Ilya Shpitser	John Hopkins		US	UCLA, Judea Pearl
<b>Oregon State University</b>				
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Bernhard Schölkopf	MPI Tübingen	Vladimir Vapnik	Tübingen, Germ	TU Berlin
Ulrike von Luxburg	MPI Tübingen		Tübingen, Germany	
Michel Besserve				



After having seen all this, we realize..

*“As X-rays are to the surgeon, graphs are for causation.”*

-Judea Pearl in Causality (2009)

